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## Math at Home

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To the Teacher

This Practice and Homework Book provides reinforcement of the concepts and skills explored in the Pearson *Math Makes Sense 5* program.

There are two sections in the book. The first section follows the sequence of *Math Makes Sense 5* Student Book. It is intended for use throughout the year as you teach the program. A two-page spread supports the content of each core lesson in the Student Book.

**In each Lesson:**

- **Quick Review** summarizes the math concepts and terminology of the Student Book lesson.
- **Try These** presents questions the student can use to check understanding of the math concepts and skills in each lesson.
- **The right page is the “homework” page, to be completed by the student with the assistance of a family member.
- **Quick Review** summarizes the math concepts and terminology of the Student Book lesson.
- **Stretch Your Thinking** presents an extension question.

**Math at Home**

The second section of the book, on pages 127 to 138, consists of 3 pull-out *Math at Home* magazines. These fun pages contain intriguing activities, puzzles, rhymes, and games to encourage home involvement. The perforated design lets you remove, fold, and send home this eight-page magazine after the student has completed Units 3, 6, and 8.
To the Family

This book will help your child practise the math concepts and skills that have been explored in the classroom. As you assist your child to complete each page, you have an opportunity to become involved in your child’s mathematical learning.

The left page of each lesson contains a summary of the main concepts and terminology of the lesson. Use this page with your child to review the work done in class. The right page contains practice.

Here are some ways you can help:

• With your child, read over the Quick Review. Encourage your child to talk about the content and explain it to you in his or her own words.
• Read the instructions with (or for) your child to ensure your child understands what to do.
• Encourage your child to explain his or her thinking.
• Some of the pages require specific materials. You may wish to gather items such as a centimetre ruler, index cards, a measuring tape, scissors, number cubes labelled 1 to 6, and paper clips.

Many of the Practice sections contain games that will also improve your child’s math skills. You may have other ideas for activities your child can share with the rest of the class.

The Math at Home pull-out pages 127 to 138 provide more fun activities.
Quick Review

Here is a number pattern: 1 2 5 10 17
A pattern rule is:
Start at 1. Add 1. Increase the number you add by 2 each time.

Here is another number pattern: 2 4 7 9 12
A pattern rule is:
Start at 2. Alternately add 2, then add 3.

Here is another number pattern: 4 8 7 11 10
A pattern rule is:
Start at 4. Alternately add 4, then subtract 1.

Try These

1. Write the next 5 terms in each pattern.
   a) 25, 29, 30, 34, 35, _____, _____, _____, _____, _____
   b) 3, 4, 6, 9, 13, _____, _____, _____, _____, _____
   c) 16, 19, 17, 20, 18, _____, _____, _____, _____, _____

2. Write the first 4 terms of each pattern.
   a) Start at 6. Add 7 each time.
       _____, _____, _____, _____
   b) Start at 2. Alternately add 6, then subtract 2.
       _____, _____, _____, _____
Practice

Use a calculator when it helps.

1. Write the next 4 terms in each pattern. Write each pattern rule.

   a) 100, 125, 120, 145, 140, ______, ______, ______, ______

      Pattern rule: ________________________________________________

   b) 85, 81, 90, 86, 95, ______, ______, ______, ______

      Pattern rule: __________________________________________________

   c) 36, 72, 144, 288, 576, _______, _______, _______, ______

      Pattern rule: __________________________________________________

2. Write the 6th term of each pattern.

   a) Start at 500. Alternately add 50, then subtract 15. __________________

   b) Start at 85. Add 7. Increase the number you add by 3 each time. _______

   c) Start at 763. Subtract 13 each time. ____________________________

   d) Start at 97. Alternately subtract 9, then add 2. ____________________

3. Start at 999. Write the first 7 terms of a pattern.

   Write the pattern rule.

   Pattern: ______________________________________________________

   Pattern rule: ______________________________________________________

Stretch Your Thinking

Write the first 5 terms of as many different patterns as you can that start with the terms 19, 24, …

___________________________________________________________________

___________________________________________________________________

___________________________________________________________________

___________________________________________________________________

___________________________________________________________________
Try These

1. One concert ticket costs $11.
   a) Complete the table to find the cost of 7 tickets.
   b) Write a pattern rule for the cost.
   c) Predict the cost of 10 tickets.
   d) Extend the pattern. How many tickets can you buy with $155?
Practice

1. Ivo practises the guitar 25 minutes every day.
   a) Make a table to show how many minutes Ivo practises in one week.
   b) How many minutes does Ivo practise in 10 days?
       ______________________
   c) How many minutes will Ivo practise in November?
       ______________________
       How many hours is that?
       ______________________
   d) How many days will it take Ivo to practise a total of 15 hours? ______

2. One minibus holds 18 students.
   a) Make a table to show how many students can ride in 6 minibuses.
   b) Write a pattern rule for the number of students.
       ______________________
       ______________________
   c) How many students can ride in 10 minibuses?
       ______________________

Stretch Your Thinking

Think about the minibuses in question 2 above.
   a) How many students can ride in 25 minibuses? ______________________
   b) How many minibuses are needed for 170 students? ___________________
Using a Variable to Describe a Pattern

Quick Review

➤ Look at the pattern and the table.

<table>
<thead>
<tr>
<th>Figure Number</th>
<th>Number of Squares</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>4 = 1 + 3</td>
</tr>
<tr>
<td>2</td>
<td>5 = 2 + 3</td>
</tr>
<tr>
<td>3</td>
<td>6 = 3 + 3</td>
</tr>
<tr>
<td>4</td>
<td>7 = 4 + 3</td>
</tr>
<tr>
<td>5</td>
<td>8 = 5 + 3</td>
</tr>
</tbody>
</table>

The number of squares is 3 more than the figure number.
Let the variable \( f \) represent any figure number:
Number of squares: \( f + 3 \)
\( f + 3 \) is an expression. It represents the pattern in the number of squares.

Try These

1. For the pattern below:
   a) Complete the table.

   Figure 1
   Figure 2
   Figure 3
   Figure 4
   Figure 5

<table>
<thead>
<tr>
<th>Figure Number</th>
<th>Number of Squares</th>
</tr>
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</table>

   b) Write an expression to represent the pattern in the numbers of squares.
Practice

1. For the pattern below:
   a) Complete the table.

<table>
<thead>
<tr>
<th>Figure</th>
<th>Number of Squares</th>
</tr>
</thead>
<tbody>
<tr>
<td>Figure 1</td>
<td></td>
</tr>
<tr>
<td>Figure 2</td>
<td></td>
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<tr>
<td>Figure 3</td>
<td></td>
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<tr>
<td>Figure 4</td>
<td></td>
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<tr>
<td>Figure 5</td>
<td></td>
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</tbody>
</table>

   b) Write an expression to represent the pattern in the number of squares.
   _________________________________

   c) Find the number of squares in the 10th figure. _______________

2. For each table, write an expression for the number of dots in any figure.

   a) | Figure Number | Number of Dots |
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>7</td>
</tr>
<tr>
<td>2</td>
<td>8</td>
</tr>
<tr>
<td>3</td>
<td>9</td>
</tr>
<tr>
<td>4</td>
<td>10</td>
</tr>
<tr>
<td>5</td>
<td>11</td>
</tr>
</tbody>
</table>

   b) | Figure Number | Number of Dots |
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
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<td>2</td>
<td>3</td>
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<td>3</td>
<td>4</td>
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<td>4</td>
<td>5</td>
</tr>
<tr>
<td>5</td>
<td>6</td>
</tr>
</tbody>
</table>

3. a) Write an expression for the number pattern.
   11, 12, 13, 14, 15, 16, . . . ______________________________

   b) Write the next 5 terms in the pattern. ______________________________

   Stretch Your Thinking

Find the 50th term in each pattern in question 2 above.

   a) __________________    b) __________________
Quick Review

Sometimes we write an equation to help us solve a problem. We use a letter variable to represent what we do not know.

Sho spent 24 hours fishing this week. He fished for 6 hours each day. How many days did Sho go fishing?

Let \( d \) represent the number of days Sho went fishing. Here are 2 equations we can write:

- We know that:
  \[
  6 \text{ hours} \times \text{ number of days fishing} = \text{total number of hours}
  \]
  \[
  6d = 24 \quad \text{or} \quad 6d = 24
  \]

- We know that:
  \[
  \text{Number of days fishing} = \text{total number of hours} \div 6
  \]
  \[
  d = 24 \div 6
  \]

Try These

Write an equation for each question.

1. Kiki caught 16 salmon. She caught 7 on Tuesday and the rest on Thursday. How many salmon did Kiki catch on Thursday? 

2. David counted 45 walruses basking in the sun. This was 3 times as many walruses as he saw last week. How many walruses did David see last week?

3. Candice built 4 models with building blocks. Each model had the same number of blocks. Altogether, Candice used 96 building blocks. How many blocks did she use for each model?
Practice
Write two equations for each question.

1. Olivia's family drove to Yellowknife, a distance of about 620 km. They drove 376 km the first day. How much farther did they have to go?

________________________________________________________________
________________________________________________________________

2. Tameko had $165. He spent $133 on a new pair of ski boots. How much money did Tomeko have left?

________________________________________________________________
________________________________________________________________

3. For gymnastics class, 72 children signed up. The children were put into teams of 8. How many teams were there?

________________________________________________________________
________________________________________________________________

4. A full bottle of water fills 6 glasses. How many bottles will serve 42 people?

________________________________________________________________
________________________________________________________________

5. Vassiliki and Gyamfi made 42 dream catchers. That was twice as many dream catchers as Petra and Yao made. How many dream catchers did Petra and Yao make?

________________________________________________________________
________________________________________________________________

Stretch Your Thinking
Write a word problem you can solve by writing an equation. Write as many equations as you can for your problem.

________________________________________________________________
________________________________________________________________

9
Quick Review
Libby makes 42 squares for a new quilt.
She needs 70 squares altogether.
How many more squares must Libby make?
Let $s$ represent the number of squares Libby has to make.
One equation is: $70 = 42 + s$
Solve the equation:
Which number do we add to 42 to get 70?
Subtract to find out: $70 - 42 = 28$
So, $s = 28$
Libby must make 28 more squares.

Try These

1. Solve each equation.
   a) $18 = m + 4$ ________________
   b) $20 = y + 14$ ________________
   c) $37 = p - 4$ ________________
   d) $53 - d = 37$ ________________

2. Write an equation. Then solve.
   a) Eli buys 36 bottles of water. He drinks 15 bottles. How many bottles are left?

   _______________________________________________________________
   _______________________________________________________________

   b) Sandra received 41 e-mails this week. Sandra received 73 e-mails altogether in two weeks. How many e-mails did Sandra receive last week?

   _______________________________________________________________
Practice

1. Solve each equation.
   a) \(43 = h + 4\) ___________________
   b) \(27 - q = 13\) _______________
   c) \(58 = 94 - n\) _______________
   d) \(76 = 23 + b\) _______________

2. For each equation in question 1, write a story problem that could be solved by using the equation.
   a) _______________________________________________________________
      _______________________________________________________________
   b) _______________________________________________________________
      _______________________________________________________________
   c) _______________________________________________________________
      _______________________________________________________________
   d) _______________________________________________________________
      _______________________________________________________________

3. Write as many equations as you can for this problem. Then solve each equation.
   Together Olga and Josef have 43 cousins. Josef has 16 cousins. How many cousins does Olga have?
   __________________________________________________________________
   __________________________________________________________________

Stretch Your Thinking

Write a story problem that could be solved by using this equation:
\(58 = f - 17\).
____________________________________________________________________
____________________________________________________________________
____________________________________________________________________
Quick Review

Kasia buys 8 tickets for a lacrosse game. Altogether the tickets cost $96. What is the cost of 1 ticket?

Let $f$ represent the cost of 1 ticket. Here are 2 equations we can write and solve.

- $f = 96 \div 8$
- $96 \div 8 = 12$
- $8 \times 12 = 96$
- So, $f = 12$

One ticket costs $12.

Try These

1. Solve each equation.
   
   a) $5p = 35$
   
   b) $5p = 50$

   c) $35 = 7m$

   d) $48 = 6k$

   e) $m = 24 \div 3$

   f) $55 \div c = 11$

   g) $h = 36 \div 6$

   h) $28 \div d = 4$

   i) $49 = 7m$

   j) $b = 72 \div 9$

2. Write an equation. Then solve.

Roger collected 6 baskets of delicious apples. Each basket held 12 apples. How many apples did Roger collect?
1. Write an equation. Solve the equation to solve the problem.

   a) Ye-Li bought an album to display her 96 hockey cards. She put 8 cards on each page. How many pages did Ye-Li fill?

   b) Katy sold 13 tickets for the harvest dance. Madhir sold twice as many tickets as Katy. How many tickets did Madhir sell?

   c) It took Marcello 3 hours to walk 12 km. About how far did Marcello walk each hour?

   d) It took a work crew 3 days to pave 24 km of highway. About how much of the highway did the crew pave each day?

2. a) Write a story problem that could be solved by using this equation: \( m \div 6 = 5 \).

   b) Solve the problem in part a.

Stretch Your Thinking

Write an equation. Write a story problem that can be solved by solving the equation.
Numbers to 100 000

Quick Review

➢ 10 000 is 10 times as great as 1000.
➢ 10 000 is 100 times as great as 100.
➢ 10 000 is 1000 times as great as 10.
➢ 10 000 is 10 000 times as great as 1.

A place-value chart shows the values of the digits in a number. As you move to the left each place value is 10 times as great as the place value before.

<table>
<thead>
<tr>
<th>Ten Thousands</th>
<th>Thousands</th>
<th>Hundreds</th>
<th>Tens</th>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>2</td>
<td>6</td>
<td>3</td>
<td>5</td>
</tr>
</tbody>
</table>

50 000 2000 600 30 5

Try These

1. Find the number of tens in:
   a) 10 ______  b) 100 ______  c) 1000 ______  d) 10 000 ______

2. Find the number of hundreds in:
   a) 100 ______  b) 1000 ______  c) 10 000 ______  d) 100 000 ______

3. Find the number of thousands in:
   a) 1000 ______  b) 10 000 ______  c) 100 000 ______

4. a) How many tens are there in 30 000? ______________
    b) How many hundreds are there in 30 000? ______________
    c) How many thousands are there in 30 000? ______________

5. Use only the digits 2, 5, and 9.
   Write a number greater than 50 000. ______________
Practice

1. How many of each would make 7000?
   a) ones  _____  b) tens  _____  c) hundreds  _____  d) thousands  _____

2. How many of each would make 60 000?
   a) tens  _____  b) hundreds  _____  
   c) thousands  _____  d) ten thousands  _____

3. For each number below, how many packages of pencils will there be?
   a) 100  ___________  b) 1000  ___________  
   c) 10 000  ___________  d) 100 000  ___________

4. Santana packs 100 booklets into each box. 
Find the number of boxes Santana will need for:
   a) 1000 booklets  _____  b) 3000 booklets  _____  c) 13 000 booklets  _____  
   d) 40 000 booklets  _____  e) 800 booklets  _____  f) 11 000 booklets  _____

5. How many of each would make $90 000?
   a) $100 bills  ___________  b) $10 bills  ___________  c) loonies  ___________

6. Sylvester earns $100 a month working at the car wash.
How many months will it take Sylvester to earn $1000?  ___________

7. How many centimetres of string would you have for each length?
   a) 6 m of string  ___________  b) 9 m of string  ___________
   c) 15 m of string  ___________  d) 23 m of string  ___________

8. Fergus bought 28 booklets of stamps. Each booklet had 10 stamps. How
many stamps did Fergus buy?  ___________

Stretch Your Thinking

How long, in centimetres, would a line of 1000 Base Ten rods be? Explain.

___________________________________________________________________
___________________________________________________________________

15
Exploring One Million

Quick Review

➤ One **million** is 1000 thousands.

Here are some benchmarks for 1 million.

- 1,000,000 s is about 12 days.
- 1,000,000 dimes = $100,000
- 1,000,000 cm = 10,000 m
- 1,000,000 days is about 2740 years.

Try These

Use a calculator when it helps.

1. Suppose you save $100 a month. How many months would it take you to save $1 million?

2. In its lifetime, a ladybug can eat about 50,000 aphids. How many ladybugs would it take to eat about 1 million aphids?

3. How many days would it take to walk 1 million metres if you walked about 4000 m per day?
Practice

1. Are there more than 1 million or less than 1 million:
   a) grains of sand on a beach? _____________________
   b) books in your classroom? _____________________
   c) blades of grass on a golf course? _____________________

2. How many of each would make $1 million?
   a) $100 bills __________
   b) $50 bills __________
   c) $20 bills __________
   d) $10 bills __________
   e) $5 bills __________
   f) toonies __________
   g) quarters __________
   h) dimes __________
   i) nickels __________

3. Suppose you read 1000 pages a month. How long would it take you to read 1 million pages?

4. How many boxes of paper clips would you need to get each number?
   a) 10 000 _________
   b) 100 000 _________
   c) 500 000 _________
   d) 1 000 000 _________

5. a) Suppose 1 bamboo skewer is about 30 cm long. How many skewers would it take to make a line 1 million centimetres long?

   b) How long would the line be in m? __________

Stretch Your Thinking

Do you think many people live to be 1 million hours old? Explain how you know.
Representing Numbers

Quick Review
Here are some ways to represent the number 987 648:

➤ Use a place-value chart.

<table>
<thead>
<tr>
<th>Hundred Thousands</th>
<th>Ten Thousands</th>
<th>Thousands</th>
<th>Hundreds</th>
<th>Tens</th>
<th>Ones</th>
</tr>
</thead>
<tbody>
<tr>
<td>9</td>
<td>8</td>
<td>7</td>
<td>6</td>
<td>4</td>
<td>8</td>
</tr>
</tbody>
</table>

900 000 + 80 000 + 7000 + 600 + 40 + 8

➤ Use expanded form.

987 648 = (9 x 100 000) + (8 x 10 000) + (7 x 1000) + (6 x 100) + (4 x 10) + (8 x 1)

900 000 + 80 000 + 7000 + 600 + 40 + 8

➤ Use words.

987 648 is nine hundred eighty-seven thousand six hundred forty-eight.

➤ Use standard form.

987 648 is written in standard form.

Try These

1. Record each number in the place-value chart.
   a) 584 628      b) 193 485      c) 76 324      d) 809 241

<table>
<thead>
<tr>
<th>Hundred Thousands</th>
<th>Ten Thousands</th>
<th>Thousands</th>
<th>Hundreds</th>
<th>Tens</th>
<th>Ones</th>
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</thead>
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<td>a)</td>
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<td>d)</td>
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</table>
Practice

1. Write each number in expanded form.
   a) 27 254
   b) 856 029
   c) 613 875

2. Write each number in question 1 in words.
   a)
   b)
   c)

3. Write each number in standard form.
   a) thirty-six thousand two hundred eight
   b) 300 000 + 20 000 + 5000 + 300 + 40 + 4

4. Write the values of each underlined digit.
   a) 575 184
   b) 874 372
   c) 105 628

5. Use the number in the box. Write the digit in the place named.

   a) ten thousands
   b) tens
   c) hundreds
   d) hundred thousands
   e) ones
   f) thousands

Stretch Your Thinking

Represent and describe the number 791 284 in as many ways as you can.

___________________________________________________________________

___________________________________________________________________

___________________________________________________________________

___________________________________________________________________
Quick Review

Here are some strategies for estimating a sum.

To estimate 41 376 + 20 443:

► Use **front-end rounding**:

41 376 + 20 443 is about 40 000 + 20 000 = 60 000.

To get a closer estimate, adjust the front-end estimate:

41 376 + 20 443 is about 41 000 + 20 000 = 61 000.

► Use **compatible numbers**:

Write 41 376 + 20 443 as:

41 300 + 20 400 = 61 700

► To estimate 4365 + 2934 + 8223 + 3785:

Use front-end rounding:

4000 + 3000 + 8000 + 4000 = 17 000

To adjust the estimate, use **compensation**:

4365 + 2934 + 8223 + 3785

4000 + 3000 + 8000 + 4000 = 19 000

Try These

Estimate each sum. Show your work.

1. a) 2893 + 6142 ____________________________
   b) 2005 + 3941 ____________________________
   c) 6734 + 985 _____________________________
   d) 1762 + 4827 + 3995 + 2042 ____________________________

2. a) Estimate: 8247 + 9468 ____________________________
   b) Use compensation to get a closer estimate.
      ____________________________
**Practice**

Play this game with a partner. Take turns.

- Circle 2 numbers in the box.
- Use a calculator to add the numbers you circled.
- Use the chart to find how many points you get.
- Continue to play until all the numbers have been used.

```
<table>
<thead>
<tr>
<th>Where Sum Falls</th>
<th>Points You Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>10 000 – 14 000</td>
<td>1</td>
</tr>
<tr>
<td>14 000 – 18 000</td>
<td>2</td>
</tr>
<tr>
<td>18 000 – 22 000</td>
<td>3</td>
</tr>
<tr>
<td>22 000 – 26 000</td>
<td>4</td>
</tr>
</tbody>
</table>
```

| 9004 | 5246 | 8312 |
| 10 356 | 6084 | 6524 | 7642 | 14 932 |
| 5285 | 11 004 | 8601 | 10 414 |
| 10 323 | 11 002 | 9734 | 8205 |
|       |       | 7602 |

**Stretch Your Thinking**

The estimated sum of two numbers is 20 000. What might the numbers be? Give two different answers.

________________________________________________________________________

________________________________________________________________________

21
Quick Review

To write an estimate for the number 17 823, you can find the closest benchmark:

In thousands: 17 823 is between 17 000 and 18 000.
   It is closer to 18 000.
   So, an estimate for 17 823 is 18 000.

In hundreds: 17 823 is between 17 800 and 17 900.
   It is closer to 17 800.
   So, a closer estimate for 17 823 is 17 800.

In tens: 17 823 is between 17 820 and 17 830.
   It is closer to 17 820.
   So, a very close estimate for 17 823 is 17 820.

Try These

1. Estimate to the nearest thousand.
   a) 5846 ________
   b) 24 237 ________
   c) 59 300 ________
   d) 43 594 ________
   e) 6147 ________
   f) 68 946 ________

2. Estimate to the nearest hundred.
   a) 8426 ________
   b) 27 729 ________
   c) 2845 ________
   d) 96 324 ________
   e) 57 691 ________
   f) 4556 ________

3. Estimate to the nearest ten.
   a) 1582 ________
   b) 6928 ________
   c) 68 793 ________
   d) 5446 ________
   e) 37 284 ________
   f) 6379 ________

4. Write an estimate for 15 941 to the nearest:
   a) thousand ________
   b) hundred ________
   c) ten ________
Practice

1. Write 3 numbers for which 9000 is an estimate.
   _______ _______ _______

2. Write 3 numbers for which 27 800 is an estimate.
   _______ _______ _______

3. Write 3 numbers for which 84 760 is an estimate.
   _______ _______ _______

4. Sanjaya is buying bottles of water for his boy scout troop. There are 38 scouts in the troop. Bottles of water are sold in packs of 6. How many 6-packs should Sanjaya buy so that each boy gets 1 bottle? Explain.
   ___________________________________________________________________
   ___________________________________________________________________
   ___________________________________________________________________
   ___________________________________________________________________

5. The 2001 population of Iqaluit was 5236. Find the closest benchmark for each:
   in thousands _______ in hundreds _______ in tens _______

6. The world record for the largest collection of bookmarks is 71 235 bookmarks. Find the closest benchmark for each:
   a) in thousands _______________
   b) in hundreds _______________
   c) in tens _______________

7. Kevin Cook has a collection of 11 097 dice. Write the closest benchmark for this number in hundreds and in tens.
   _______ _______

Stretch Your Thinking

Write a number that has the same estimate when using benchmarks in thousands and in hundreds. _______________
How did you find your number? ____________________________________________
   ___________________________________________________________________
Estimating Differences

Quick Review

Here are some strategies for estimating a difference.

➢ To estimate 6702 – 3494:
  Use front-end rounding.
  6702 – 3494 is about 6000 – 3000 = 3000.
  To get a closer estimate, look at the last 3 digits of each number.
  702 is about 700.
  494 is about 500.
  700 – 500 = 200
  Add 200 to the estimate of 3000: 3000 + 200 = 3200
  So, 6702 – 3494 is about 3200.

➢ To estimate 5707 – 212:
  Use compatible numbers.
  5707 is close to 5712;
  then, 5712 – 212 = 5500
  Or, 212 is close to 207;
  then, 5707 – 207 = 5500

➢ To estimate 3284 – 1935:
  Estimate each number to the closest 1000: 3000 – 2000 = 1000
  To get a closer estimate, estimate each number to the closest hundred:
  3300 – 1900 = 1400

Try These

1. Estimate each difference. Use any strategy you wish.
   a) 6842 – 439 ____________  b) 9527 – 2476 ____________
   c) 7654 – 1235 ____________  d) 7024 – 891 ____________
   e) 4593 – 2861 ____________  f) 3782 – 422 ____________

2. Use front-end rounding to estimate each difference.
   a) 2936 – 481 ____________  b) 8236 – 3719 ____________
1. Use front-end rounding to estimate each difference.
   a) $3842 - 2137$ __________ 
   b) $8204 - 938$ __________
   c) $7934 - 4836$ __________ 
   d) $7835 - 5934$ __________ 

2. Use compatible numbers to estimate each difference.
   a) $7634 - 5842$ __________ 
   b) $8378 - 167$ __________ 
   c) $9788 - 2473$ __________ 
   d) $5602 - 410$ __________ 

3. Jennah has 1250 flyers to deliver. So far, she has delivered 527. About how many flyers does Jennah still have to deliver?
   ______________________

4. Use the data in the table. Estimate each difference.
<table>
<thead>
<tr>
<th>Day</th>
<th>Number Sold</th>
</tr>
</thead>
<tbody>
<tr>
<td>Monday</td>
<td>964</td>
</tr>
<tr>
<td>Tuesday</td>
<td>709</td>
</tr>
<tr>
<td>Wednesday</td>
<td>1432</td>
</tr>
<tr>
<td>Thursday</td>
<td>1031</td>
</tr>
<tr>
<td>Friday</td>
<td>1936</td>
</tr>
<tr>
<td>Saturday</td>
<td>2262</td>
</tr>
</tbody>
</table>

   a) About how many more tickets were sold on Friday than on Monday? __________
   b) About how many more tickets were sold on Wednesday than on Tuesday? __________
   c) About how many more tickets were sold on Saturday than on Thursday? __________

5. Toby estimated that $3676 - 493$ was 3100. Was Toby’s estimate high or low? Which estimation strategy do you think Toby used?
   _______________________________________________________________________
   _______________________________________________________________________

Stretch Your Thinking

Two 4-digit numbers have a difference of about 1900. What might the two numbers be?
   _______________________________________________________________________
   _______________________________________________________________________
Using Estimation to Check Answers

**Quick Review**

Here is one way to add: 3510 + 2637

\[
\begin{align*}
3000 + 2000 &= 5000 \\
500 + 600 &= 1100 \\
10 + 37 &= \text{47} \\
&= \text{6147}
\end{align*}
\]

To check this sum is reasonable, you can use estimation. Compensate by rounding one number up and the other number down:

- 3510 rounds down to 3500.
- 2637 rounds up to 2700.

\[3500 + 2700 = 6200.\]

Since 6200 is close to 6147, the answer is reasonable.

Here is one way to subtract: 4760 – 2496

Count on from 2496 to 4760.

\[
\begin{array}{ccccccc}
2496 & 2500 & 3000 & 4000 & 4700 & 4760 \\
+4 & +500 & +1000 & +700 & +60 &= 2264
\end{array}
\]

So, 4760 – 2496 = 2264

To check this difference is reasonable, estimate: 4760 – 2460 = 2300

2300 is close to 2264, so the answer is reasonable.

**Try These**

1. Add or subtract. Estimate to check. Show your thinking.
   
   a) \(3472 + 5836\)  
   b) \(5279 – 3518\)
Practice

Solve each problem. Estimate to check your answers are reasonable. Show your work.

1. Marina collected 635 acorns. Urvashi collected 426.
   a) Suppose Marina and Urvashi combined their collections. How many acorns would there be?
   b) How many more acorns did Marina collect than Urvashi?

2. The CN Tower in Toronto has 1776 steps. The Menara Tower in Kuala Lumpur has 2058 steps. How many more steps than the CN Tower does the Menara Tower have?

3. Simon is a transport truck driver. Last week, Simon drove 6237 km. This week he drove 4117 km. How far did Simon drive in the 2 weeks?

Stretch Your Thinking

Use some of the data in the table to write a subtraction problem. Solve the problem. Estimate to check your answer.

<table>
<thead>
<tr>
<th>Trench</th>
<th>Depth (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mariana</td>
<td>10 911</td>
</tr>
<tr>
<td>Puerto Rico</td>
<td>9 220</td>
</tr>
<tr>
<td>Yap</td>
<td>8 527</td>
</tr>
</tbody>
</table>
Patterns in Multiplication and Division

Quick Review

Here are some strategies to help you multiply and divide.

► Skip count up or down from a known fact to multiply.
  • To find $9 \times 7$:
    Start with: $7 \times 7 = 49$
    $9 \times 7 = 49 + 7 + 7$
    = 63
    So, $9 \times 7 = 63$
  • To find $6 \times 8$:
    Start with: $8 \times 8 = 64$
    $6 \times 8 = 64 - 8 - 8$
    = 48
    So, $6 \times 8 = 48$

► Use related multiplication facts to divide.
  • To find $56 \div 7$:
    Think: $7 \times 8 = 56$
    So, $56 \div 7 = 8$
  • To find $72 \div 8$:
    Think: $8 \times 9 = 72$
    So, $72 \div 8 = 9$

Try These

1. Multiply.
   a) $9 \times 8 = ___$
   b) $4 \times 6 = ___$
   c) $7 \times 6 = ___$
   d) $6 \times 7 = ___$
   e) $5 \times 8 = ___$
   f) $8 \times 7 = ___$

2. Divide.
   a) $72 \div 9 = ___$
   b) $16 \div 2 = ___$
   c) $81 \div 9 = ___$
   d) $36 \div 4 = ___$
   e) $63 \div 9 = ___$
   f) $35 \div 5 = ___$

3. Write a related multiplication fact for each division.
   a) $64 \div 8$ ________________
   b) $42 \div 7$ ________________
   c) $27 \div 3$ ________________
   d) $30 \div 6$ ________________

4. Write as many related facts as you can for each set of numbers.
   a) $6, 7, 42$ _______________________
   b) $6, 9, 54$ _______________________

28
Practice

Play this game with a partner.
You will need:
counters of 2 colours
2 number cubes labelled 4 to 9

Take turns.
► Roll the number cubes and multiply the numbers that come up.
   Cover the product on the game board with one of your counters.
► The first player to cover 4 products in a vertical, horizontal, or diagonal line wins.

<table>
<thead>
<tr>
<th>81</th>
<th>32</th>
<th>25</th>
<th>48</th>
<th>20</th>
</tr>
</thead>
<tbody>
<tr>
<td>42</td>
<td>72</td>
<td>49</td>
<td>36</td>
<td>40</td>
</tr>
<tr>
<td>54</td>
<td>30</td>
<td>16</td>
<td>64</td>
<td>32</td>
</tr>
<tr>
<td>24</td>
<td>56</td>
<td>72</td>
<td>45</td>
<td>81</td>
</tr>
<tr>
<td>63</td>
<td>35</td>
<td>28</td>
<td>64</td>
<td>36</td>
</tr>
</tbody>
</table>

Stretch Your Thinking

Write as many division facts as you can that have a quotient of 8.

__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
Other Strategies for Multiplying and Dividing

Quick Review
You can use doubling and repeated doubling to multiply.

- Begin with a fact that you know.
  - To find another fact, double one factor, then double the product.
    - $3 \times 8 = 24$
    - Double one factor: $3 \times 8 = 24$
    - Double the product: $6 \times 8 = 48$
  - To find $4 \times 9$:
    - You know $2 \times 9 = 18$
    - So, $4 \times 9 = 18 + 18 = 36$

You can use halving and repeated halving to divide.

- To find $36 \div 4$:
  - Think: $4$ is $2 \times 2$.
  - So, to divide by $4$, I can divide by $2$, then divide by $2$ again.
    - $36 \div 2 = 18$
    - $18 \div 2 = 9$
    - So, $36 \div 4 = 9$

- To find $88 \div 8$:
  - Think: $8$ is $4 \times 2$ and $4$ is $2 \times 2$.
  - So, to divide by $8$, I can divide by $2$, then divide by $2$, then divide by $2$ again.
    - $88 \div 2 = 44$
    - $44 \div 2 = 22$
    - $22 \div 2 = 11$
    - So, $88 \div 8 = 11$

Try These

1. Use doubling to find each product.
   - a) $8 \times 7$
   - b) $6 \times 5$
   - c) $9 \times 4$
   - d) $6 \times 7$

2. Use halving to divide.
   - a) $48 \div 4$
   - b) $24 \div 4$
1. Multiply. Then find a new fact by doubling the first factor in each pair.
   a) $5 \times 7 = ___$  
      ______________________
   b) $3 \times 8 = ___$  
      ______________________
   c) $4 \times 9 = ___$  
      ______________________
   d) $2 \times 16 = ___$  
      ______________________

2. Use halving or repeated halving to divide.
   a) $48 \div 4$  
      ______________________________________________________
   b) $64 \div 8$  
      ______________________________________________________
   c) $56 \div 8$  
      ______________________________________________________
   d) $36 \div 4$  
      ______________________________________________________

3. Divide by 2 to find $32 \div 8$. Show all the steps.
   $32 \div 8$  
   ______________________________________________________

4. Draw an array to show repeated halving to divide.
   
   | 64 $\div 8 = ___$ | 80 $\div 8 = ___$ |

5. How can you use $3 \times 7$ to find $6 \times 7$?  
   ______________________________
   ______________________________________________________

Stretch Your Thinking

a) Why can you not use halving to find $49 \div 7$?
   ______________________________________________________

b) Which strategy could you use?
   ______________________________________________________
Multiplying with Multiples of 10

Quick Review

- Use place value to multiply by 10, 100, and 1000.
  
  Find each product: \( 31 \times 10 \quad 31 \times 100 \quad 31 \times 1000 \)

  - \( 31 \times 1 \text{ ten} = 31 \text{ tens} \)
  - \( 31 \times 1 \text{ hundred} = 31 \text{ hundreds} \)
  - \( 31 \times 1 \text{ thousand} = 31 \text{ thousands} \)

- Use basic facts to multiply by multiples of 10, 100, and 1000.
  
  Find each product: \( 6 \times 400 \quad 6 \times 4000 \)

  - You know \( 6 \times 4 = 24 \)
  - \( 6 \times 4 \text{ hundreds} = 24 \text{ hundreds} \)
  - So, \( 6 \times 400 = 2400 \) \( 6 \times 4000 = 24000 \)

- Multiply 2 multiples of 10, 100, and 1000.
  
  Find each product: \( 40 \times 20 \quad 300 \times 60 \)

  - \( 4 \text{ tens} \times 20 = 80 \text{ tens} \)
  - \( 3 \text{ hundreds} \times 60 = 180 \text{ hundreds} \)
  - \( 40 \times 20 = 800 \) \( 300 \times 60 = 18000 \)

Try These

1. Multiply.
   
   a) \( 38 \times 10 = \) \( \quad \)
   
   b) \( 73 \times 10 = \) \( \quad \)
   
   c) \( 30 \times 10 = \) \( \quad \)

   - \( 38 \times 100 = \)
   
   - \( 73 \times 100 = \)
   
   - \( 30 \times 100 = \)

   - \( 38 \times 1000 = \)
   
   - \( 73 \times 1000 = \)
   
   - \( 30 \times 1000 = \)

   d) \( 6 \times 9 = \) \( \quad \)
   
   e) \( 12 \times 8 = \) \( \quad \)
   
   f) \( 9 \times 7 = \) \( \quad \)

   - \( 6 \times 90 = \)
   
   - \( 12 \times 80 = \)
   
   - \( 9 \times 70 = \)

   - \( 6 \times 900 = \)
   
   - \( 12 \times 800 = \)
   
   - \( 9 \times 700 = \)

   - \( 6 \times 9000 = \)
   
   - \( 12 \times 8000 = \)
   
   - \( 9 \times 7000 = \)

2. Find each product.
   
   a) \( 40 \times 30 = \) \( \quad \)
   
   b) \( 80 \times 50 = \) \( \quad \)
   
   c) \( 20 \times 70 = \) \( \quad \)
Practice

1. Multiply.
   a) \(43 \times 10 = \) ________  
   b) \(7 \times 90 = \) ________  
   c) \(50 \times 70 = \) ________  
      \(43 \times 100 = \) ________  
      \(7 \times 900 = \) ________  
      \(50 \times 700 = \) ________  
      \(43 \times 1000 = \) ________  
      \(7 \times 9000 = \) ________  
      \(50 \times 7000 = \) ________

2. Find each product.
   a) \(35 \times 100 = \) ________  
   b) \(14 \times 900 = \) ________  
   c) \(12 \times 70 = \) ________  
      \(17 \times 2000 = \) ________  
      \(20 \times 80 = \) ________  
      \(11 \times 8000 = \) ________

3. Find the total value of each set of bills.
   a) eighty $10 bills ________  
   b) sixty $20 bills ______________
   c) seventy $50 bills ________  
   d) nine hundred $100 bills ______________

4. A hamster eats 11 g of food a day. How much food does it eat in the month of April?
   \(\) _____________________________________________________________________

5. Margie packed 80 pamphlets in each of 70 envelopes. How many pamphlets did she pack?
   \(\) _____________________________________________________________________

6. Tickets to a concert cost $40 each. How much do 90 tickets cost?
   \(\) _____________________________________________________________________

7. A theatre has 60 rows of 30 seats. How many seats is that altogether?
   \(\) _____________________________________________________________________

Stretch Your Thinking

A payroll clerk writes 20 cheques for $600 and 12 cheques for $400. What is the total amount of the cheques?
   \(\) _____________________________________________________________________
   \(\) _____________________________________________________________________
Estimating Products to Solve Problems

Quick Review

Here are some strategies to help you estimate products.

➤ Use compatible numbers.
   Estimate: \(27 \times 9\)
   Think: \(30 \times 9 = 270\)
   Or, \(27 \times 10 = 270\)
   Or, \(30 \times 10 = 300\)

➤ Use compatible numbers and compensation.
   Estimate: \(48 \times 31\)
   Think: \(50 \times 30 = 1500\)

➤ Use front-end rounding:
   Estimate: \(7 \times 316\)
   Think \(7 \times 300 = 2100\)

When we round one number up and one number down, we have used compensation.

Since 300 is less than 316, then 2100 is an underestimate.

Try These

1. Use compatible numbers to estimate each product.
   a) \(9 \times 78\) _______________
   b) \(583 \times 8\) _______________
   c) \(62 \times 79\) _______________
   d) \(82 \times 12\) _______________

2. Estimate each product.
   a) \(68 \times 9\) _______________
   b) \(314 \times 5\) _______________
   c) \(7 \times 223\) _______________
   d) \(8 \times 218\) _______________

3. Tell if each estimate in question 2 is an overestimate or an underestimate.
   a) __________________________
   b) __________________________
   c) __________________________
   d) __________________________
Solve each problem. Show your work.

1. There are 24 marchers in each row. There are 58 rows of marchers. About how many marchers are there?

2. Chintana and her family make 48 ookpiks each month. About how many ookpiks do they make in one year?

3. Each box contains 132 tissues. About how many tissues are in 18 boxes?

4. The estimated answer to a multiplication question is 5100. What might the question be?

5. Approximately 380 people visit the children’s museum each day. About how many people visit the children’s museum in 7 days?

6. Roy estimated the product of 587 × 8 to be about 4800. Which strategy did Roy use?

**Stretch Your Thinking**

Write a story problem for which an overestimate would be appropriate.
Using Mental Math to Multiply

Quick Review
Here are some strategies for multiplying mentally.

- **Multiply**: $6 \times 18$
  - $6 \times 8 = 48$
  - $6 \times 10 = 60$
  - $48 + 60 = 108$
  - $6 \times 18 = 108$

- **Multiply**: $24 \times 35$
  - $24 = 12 \times 2$
  - $24 \times 35 = 12 \times 3 \times 35$
    - $= 12 \times 70$
    - $= 840$
  - So, $24 \times 35 = 840$

- **Multiply**: $14 \times 15$
  - Half of 14 is 7.
  - Double 15 is 30.
  - $7 \times 30 = 210$
  - So, $14 \times 15 = 210$

- **Multiply**: $203 \times 6$
  - $200 \times 6 = 1200$
  - $3 \times 6 = 18$
  - $1200 + 18 = 1218$
  - So, $203 \times 6 = 1218$

Try These

1. Multiply. Use mental math.
   - a) $5 \times 45 = \underline{}$
   - b) $12 \times 45 = \underline{}$
   - c) $197 \times 3 = \underline{}$
   - d) $18 \times 25 = \underline{}$
   - e) $2 \times 599 = \underline{}$
   - f) $14 \times 35 = \underline{}$

2. Use mental math. Find the product of $16 \times 35$ two different ways. Describe the strategies you used.

   ______________________________________________________
   ______________________________________________________
   ______________________________________________________

3. Explain why $28 \times 25 = 7 \times 4 \times 25$.
Practice

1. Use mental math to find each product.
   a) \(12 \times 25 = \) _______
   b) \(58 \times 26 = \) _______
   c) \(402 \times 8 = \) _______
   d) \(9 \times 49 = \) _______
   e) \(36 \times 18 = \) _______
   f) \(17 \times 199 = \) _______

2. Use mental math to solve each problem.
   a) Emily has 8 books of stickers. Each book has 198 stickers. How many stickers does Emily have?
      _______________________________________________________________

   b) A grocer ordered 26 boxes of oranges. Each box contains 3 dozen oranges. How many oranges did the grocer order?
      _______________________________________________________________

   c) Suppose your heart beats 78 times a minute. How often does it beat in an hour?
      _______________________________________________________________

3. Use mental math to complete this table.

<table>
<thead>
<tr>
<th></th>
<th>25</th>
<th>16</th>
<th>42</th>
</tr>
</thead>
<tbody>
<tr>
<td>23</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>35</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>14</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>11</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Stretch Your Thinking

Which product is greater, \(25 \times 36\) or \(98 \times 9\)? How much greater?

_____________________________________________________________________
_____________________________________________________________________
Quick Review

Multiply: 32 \times 24

Here is one way to multiply:

Write each factor in expanded form.
Then write 4 partial products.

\[
32 \times 24 = (30 + 2) \times (20 + 4)
= (30 \times 20) + (30 \times 4) + (2 \times 20) + (2 \times 4)
= 600 + 120 + 40 + 8
= 768
\]

Estimate to check if the answer is reasonable:
32 \times 24 is about 30 \times 25 = 3 \times 25 \times 10
= 75 \times 10
= 750
Since 750 is close to 768, the answer is reasonable.

Try These

1. Multiply.
   a) \quad 46 \quad \times 32
   b) \quad 74 \quad \times 23
   c) \quad 14 \quad \times 18
   d) \quad 53 \quad \times 22

2. Find each product.
   a) \quad 64 \quad \times 23
   b) \quad 94 \quad \times 12
   c) \quad 82 \quad \times 26
   d) \quad 34 \quad \times 33
Practice

1. Play this game with a partner.
   You will need 10 cards labelled 0 to 9, placed in a paper bag.
   - Each player draws a multiplication grid like this on paper.
     \[
     \begin{array}{c}
     \times \\
     \end{array}
     \]
   - Take turns to draw a card from the bag.
     On each draw, both players record the digit in any box on their grids.
   - Return the card to the bag after each draw.
   - Continue until all the boxes are filled.
   - Multiply using paper and pencil.
     Check each other’s product.
   - The player with the greater product wins a point.
   - Play 5 rounds to determine an overall winner.

2. Solve each problem. Show your work.
   a) Bruce jogs a total of 25 km every week.
      How many kilometres does he jog in a year?
      \[
      \text{______________________________________________________________} \\
      \text{______________________________________________________________}
      \]
   b) Nya earns $17 a week baby-sitting.
      How much does she earn in 12 weeks?
      \[
      \text{______________________________________________________________} \\
      \text{______________________________________________________________}
      \]

Stretch Your Thinking

Find 2 consecutive 2-digit numbers whose product is 812.
Estimating Quotients to Solve Problems

Quick Review

Here are some strategies you can use to estimate quotients.

➤ Estimate: $984 \div 5$
   Look for **compatible numbers**.
   $984$ is close to $1000$.
   $1000$ is $10$ hundreds.
   $10$ hundreds $\div 5 = 2$ hundreds
   $= 200$
   $984 \div 5$ is about $200$.
   This is an overestimate because $1000 > 984$.

➤ Estimate: $364 \div 5$
   Use front-end rounding.
   $364 \div 5$ is about $300 \div 5$.
   $30 \div 5 = 6$, so $300 \div 5 = 60$
   The estimate is low.
   To get a closer estimate, look at the first 2 digits of the dividend:
   $364 \div 5$
   $35 \div 5 = 7$, so $36 \div 5$ is close to $7$.
   So, $364 \div 5$ is about $350 \div 5 = 70$

Try These

1. Estimate each quotient.
   a) $273 \div 5$
   b) $942 \div 6$
   c) $470 \div 8$
   d) $984 \div 3$
   e) $789 \div 9$
   f) $447 \div 4$
Practice

1. Estimate each quotient.
   a) \(351 \div 7\)  b) \(429 \div 5\)  c) \(632 \div 8\)  d) \(472 \div 6\)
   _______  _______  _______  _______
   e) \(209 \div 4\)  f) \(221 \div 3\)  g) \(994 \div 5\)  h) \(884 \div 9\)
   _______  _______  _______  _______

2. Sydney has 893 collector’s coins. He wants to mount them in groups of 9.
   About how many groups can he make? _______________________________

3. Bruno travelled 785 km in one week.
   About how far did he travel each day? _______________________________

4. Maude made 140 g of trail mix.
   About how much can she serve to each of 8 guests? _________________

5. About how many Saturdays are there in 1 year? _____________________

6. One hundred ninety-one children signed up for basketball.
   About how many teams of 9 can the coaches make? _________________

7. Crayons are packaged in boxes of 8.
   About how many boxes can be filled with 250 crayons? _______________

Stretch Your Thinking

Arnold estimated that \(847 \div 8\) is about 100. Was his estimate high or low? Explain.

_____________________________________________________________________
_____________________________________________________________________
_____________________________________________________________________
Dividing a 3-Digit Number by a 1-Digit Number

Quick Review
To divide 158 by 4, you can subtract multiples of 4.

Choose any multiple of 4 less than 158. Start with 40.

\[
\begin{array}{c|c|c|c}
\text{Subtract} & \text{Then} & \text{Then} & \text{Add the side} \\
\text{40 from 158.} & \text{subtract 80.} & \text{subtract 36.} & \text{numbers.} \\
4)158 & 4)158 & 4)158 & 4)158 \\
- 40 & - 40 & - 40 & - 40 \\
118 & 118 & 118 & 118 \\
- 80 & - 80 & - 80 & \overline{118} \\
38 & 38 & 38 & 38 \\
\hline
- 36 & - 36 & - 36 & \overline{2} \\
\hline
2 & \overline{2} & \text{10 + 20 + 9 = 39} & \\
\end{array}
\]

4)158 is 39 with 2 left over.

Try These

1. Divide. Show your work.
   a) 3)246          b) 5)187          c) 4)861          d) 6)358

\[
\begin{array}{c|c|c|c}
\text{Try These} & \text{Try These} & \text{Try These} & \text{Try These} \\
\text{1. } & \text{1. } & \text{1. } & \text{1. } \\
\text{Divide. Show your work.} & \text{Divide. Show your work.} & \text{Divide. Show your work.} & \text{Divide. Show your work.} \\
\text{a) 3)246} & \text{b) 5)187} & \text{c) 4)861} & \text{d) 6)358} \\
\end{array}
\]
1. Divide.
   a) \(467 \div 3 = \underline{\quad}\)  
   b) \(184 \div 8 = \underline{\quad}\)  
   c) \(462 \div 9 = \underline{\quad}\)

2. Play this game with a partner.
   You will need:
   1 Base Ten unit cube or other small object

   ► Both players draw a division grid like this one:

   ► Players take turns dropping the cube onto the numbered circle with their eyes closed. In any box on the grids, both players record the number on which the cube landed.
   ► Continue until all the boxes on the grids are full.
   ► Divide.
   The player with the greater answer wins.
   Play 5 more games.

Stretch Your Thinking

Suppose you are playing the game above.
Where on your grid should you record a 9? Explain.
Here are 2 ways to divide 587 by 4.

1. Use place value.
   - Divide the hundreds.
   - Divide the tens.
   - Divide the ones.

   \[
   \begin{array}{c|c|c|c|c}
   1 & 4 & 8 & 7 \\
   \hline
   4 & 5 & 8 & 7 \\
   -4 & -4 & -1 & 6 \\
   1 & 8 & 2 & 3 \\
   \hline
   587 & 4 & 146 & R3 \\
   \end{array}
   \]

   \[
   \begin{array}{c|c|c|c|c}
   1 & 4 & 6 \\
   \hline
   4 & 5 & 8 & 7 \\
   -4 & -4 & -1 & 6 \\
   1 & 8 & 2 & 3 \\
   \hline
   587 & 4 & 146 & R3 \\
   \end{array}
   \]

   \[
   \begin{array}{c|c|c|c|c}
   1 & 4 & 6 \\
   \hline
   4 & 5 & 8 & 7 \\
   -4 & -4 & -1 & 6 \\
   1 & 8 & 2 & 3 \\
   \hline
   587 & 4 & 146 & R3 \\
   \end{array}
   \]

   \[
   \begin{array}{c|c|c|c|c}
   587 & 4 & 146 & R3 \\
   \hline
   400 & 100 & 87 \\
   \hline
   587 & 400 & 100 & 100 & 25 & 87 & 4 & 21 & R3 \\
   \hline
   587 & 146 & R3 \\
   \hline
   \end{array}
   \]

   \[
   \begin{array}{c|c|c|c|c}
   587 & 4 & 146 & R3 \\
   \hline
   400 & 100 & 87 \\
   \hline
   587 & 400 & 100 & 100 & 25 & 87 & 4 & 21 & R3 \\
   \hline
   587 & 146 & R3 \\
   \hline
   \end{array}
   \]

   To check, multiply 146 by 4, then add 3.

   \[
   \begin{array}{c|c|c|c|c}
   146 & 584 \\
   \hline
   8 & 9 \\
   \hline
   584 & 584 & 3 \\
   \hline
   587 & 587 & 604 \\
   \hline
   \end{array}
   \]

2. Use mental math.

   \[
   \begin{array}{c|c|c|c|c}
   587 & 4 & 400 & 100 & 87 \\
   \hline
   400 & 100 & 25 & 87 & 4 & 21 & R3 \\
   \hline
   587 & 146 & R3 \\
   \hline
   \end{array}
   \]

   So, 587 \div 4 = 100 + 25 + 21 + R3

   \[
   \begin{array}{c|c|c|c|c}
   587 & 4 & 146 & R3 \\
   \hline
   400 & 100 & 87 \\
   \hline
   587 & 400 & 100 & 100 & 25 & 87 & 4 & 21 & R3 \\
   \hline
   587 & 146 & R3 \\
   \hline
   \end{array}
   \]

   To check, multiply 146 by 4, then add 3.

   \[
   \begin{array}{c|c|c|c|c}
   146 & 584 \\
   \hline
   8 & 9 \\
   \hline
   584 & 584 & 3 \\
   \hline
   587 & 587 & 604 \\
   \hline
   \end{array}
   \]

   Since this is the dividend, the answer is correct.

### Try These

1. Divide.

   a) \( 6 \div 763 \)
   b) \( 4 \div 253 \)
   c) \( 5 \div 356 \)
   d) \( 2 \div 128 \)

   e) \( 3 \div 568 \)
   f) \( 7 \div 147 \)
   g) \( 8 \div 593 \)
   h) \( 9 \div 604 \)
1. Find each quotient.

   a) \( 6 \div 463 \)  
   b) \( 8 \div 589 \)  
   c) \( 5 \div 248 \)  

   d) \( 2 \div 336 \)  
   e) \( 7 \div 409 \)  
   f) \( 4 \div 632 \)  

   g) \( 3 \div 862 \)  
   h) \( 9 \div 413 \)  
   i) \( 7 \div 300 \)  

   j) \( 3 \div 584 \)  
   k) \( 6 \div 713 \)  
   l) \( 8 \div 623 \)  

2. In the cafeteria, students sit at tables for 8.
   How many tables are needed for 563 students?

   ________________________________________________

3. A ticket seller sold $272 worth of movie tickets.
   How many tickets did she sell if each ticket cost $8?

   ________________________________________________

**Stretch Your Thinking**

Use the digits 4, 6, 7, and 8 to make the greatest quotient with no remainder.
Quick Review

Maxine knits mittens and stocking caps and sells them at the market. She charges $8 for a cap and $9 for a pair of mittens. Last winter, Maxine’s sales totalled $449. She sold 25 pairs of mittens. How many caps did she sell?

First, find out how much she took in for mittens.
Multiply: $9 \times 25 = 225$
Maxine took in $225$ for mittens.

Next, find out how much Maxine took in for the caps.
Subtract: $449 - 225 = 224$
Maxine took in $224$ for caps.

Finally, find out how many caps Maxine sold.
Divide: $224 \div 8 = 28$
Maxine sold 28 stocking caps.

Try These

1. Munir worked on a farm for 3 weeks last summer. The first week, he earned $150. The second week, he earned $24 more than the first week. The third week, he earned $17 less than the second week. How much money did Munir earn altogether?

________________________________________________________________
________________________________________________________________
________________________________________________________________

2. Pan has 367 marbles. Seventy-eight marbles are green. One hundred thirty-one are red. How many marbles of other colours does Pan have?

________________________________________________________________
________________________________________________________________

46
Practice

Solve each problem. Show all your work.

1. Lonny uses 12 cups of flour to make 6 batches of cookies. How much flour will he need to make 18 batches of cookies?
   _______________________________________________________________
   _______________________________________________________________

2. Liana packed 24 novels into each of 16 boxes. She packed 28 spelling books into each of 13 boxes. How many books did Liana pack?
   _______________________________________________________________
   _______________________________________________________________
   _______________________________________________________________
   _______________________________________________________________

3. Kiara spent $273 on school clothes. She bought 2 pairs of jeans at $39 each, and 5 tops at $19 each. She spent the rest of the money on a pair of shoes. How much did Kiara spend on shoes?
   _______________________________________________________________
   _______________________________________________________________
   _______________________________________________________________
   _______________________________________________________________
   _______________________________________________________________

Stretch Your Thinking

Gene had 144 hens. He sold 48 of them to Bonny and 16 of them to Mark. How many hens does Gene have left?
   _______________________________________________________________
   _______________________________________________________________
   _______________________________________________________________
   _______________________________________________________________
Measuring Length

Quick Review
This crayon is about 6 cm long.

To be more precise, you can read the length in millimetres.
The crayon is 59 mm long.

One millimetre is one-tenth of a centimetre.
So, you can say the length in centimetres.
The crayon is 5.9 cm long.
You say: 5 and 9 tenths centimetres

10 mm = 1 cm
So, 1 mm = 0.1 cm

100 cm = 1 m
So, 1 cm = 0.01 m

1000 mm = 1 m

Try These

1. Estimate the length of each line segment to the nearest centimetre.
   Then, measure and record the actual length in millimetres and centimetres.

<table>
<thead>
<tr>
<th>Estimate (cm)</th>
<th>Length (mm)</th>
<th>Length (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>a)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>b)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>c)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Practice

1. Work with a partner.

You will need:
small objects, such as a pencil, a crayon, a paper clip, a straw, a craft stick
a 30-cm ruler

➤ Choose an object.
➤ Both of you estimate the object’s length to the nearest centimetre.
➤ Record your estimates.
➤ Measure and record the actual length in millimetres and in centimetres.
➤ Repeat with other objects.

<table>
<thead>
<tr>
<th>Object</th>
<th>Our Estimates (cm)</th>
<th>Actual Length (mm)</th>
<th>Actual Length (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Stretch Your Thinking

Measure and record the width of your hand and your foot.
Complete the chart.

<table>
<thead>
<tr>
<th>Width (mm)</th>
<th>Width (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hand</td>
<td></td>
</tr>
<tr>
<td>Foot</td>
<td></td>
</tr>
<tr>
<td>Difference</td>
<td></td>
</tr>
</tbody>
</table>
Quick Review

Rectangles with equal perimeters can have different areas. Each rectangle below has perimeter of 14 cm.

<table>
<thead>
<tr>
<th>Width</th>
<th>Area</th>
<th>Shape</th>
</tr>
</thead>
<tbody>
<tr>
<td>6 cm</td>
<td>6 cm²</td>
<td>Least width</td>
</tr>
<tr>
<td>10 cm</td>
<td>10 cm²</td>
<td></td>
</tr>
<tr>
<td>12 cm</td>
<td>12 cm²</td>
<td>Closest to square</td>
</tr>
</tbody>
</table>

The rectangle with the least width has the least area.

The rectangle closest in shape to a square has the greatest area.

Try These

1. Draw all possible rectangles with a perimeter of 18 cm. Label each rectangle with its area.
Practice

Find the perimeter and the area of each rectangle. Then draw another rectangle with the same perimeter. Record the area of the rectangle you drew.

Each small square has an area of 1 cm².

1. 

Perimeter = _______
Area = _______ Area = _______

2. 

Perimeter = _______
Area = _______

Stretch Your Thinking

Suppose the area of your rectangular garden is 5 m². What is its perimeter? Explain.
Exploring Rectangles with Equal Areas

Quick Review

Rectangles with equal areas can have different perimeters. Each rectangle below has area 12 cm².

- Perimeter: 26 cm
- Perimeter: 16 cm
- Perimeter: 14 cm

The rectangle with the least width has the greatest perimeter.

The rectangle that is closest in shape to a square has the least perimeter.

Try These

Draw all the possible rectangles with area 16 cm².
1. Draw a rectangle with each area and perimeter. Label each rectangle with its letter.
   A: area $14 \text{ cm}^2$ and perimeter $18 \text{ cm}$; B: area $24 \text{ cm}^2$ and perimeter $20 \text{ cm}$;
   C: area $36 \text{ cm}^2$ and perimeter $24 \text{ cm}$; D: area $1 \text{ cm}^2$ and perimeter $4 \text{ cm}$;
   E: area $9 \text{ cm}^2$ and perimeter $12 \text{ cm}$

2. The area of a rectangular carpet is $36 \text{ m}^2$.
   What is the least perimeter the carpet could have? _______
   What is the greatest perimeter the carpet could have? _______

**Stretch Your Thinking**

Pat needs $48 \text{ m}$ of fencing to surround her rectangular rose garden.
What could the area of Pat’s garden be? Give as many answers as you can.

___________________________________________________________________
___________________________________________________________________
Exploring Volume

Quick Review

The amount of space inside an object is a measure of its volume. You can find the volume of a container by filling it with identical items, then counting these items.

- This box holds 12 donuts. It has a volume of about 12 donuts.

- This box holds 20 floor tiles. It has a volume of 20 floor tiles.

- This container holds 9 ping-pong balls. It has a volume of about 9 ping-pong balls.

Try These

1. What is the volume of each object?
   a) 170 Cotton Swabs
   b) 36 Crayons
   c) 132 Tissues

2. Find a small box.
   Estimate the volume in Snap Cubes. Estimate: __________
   Fill the box to check your estimate. Volume: __________
**Practice**

1. What is the volume of each object?
   a) __________________
   b) __________________
   c) __________________

2. Find a small box.
   Estimate its volume in green Pattern Blocks.
   Fill the box to check your estimate.
   Repeat with orange Pattern Blocks.
   Record your work in the table.

3. Suppose you fill a box with marbles. Then you fill the same box with ping-pong balls. Would you need more marbles or more ping-pong balls to fill the box? Explain.

   _________________________________________________________________
   _________________________________________________________________

4. Which item would you use to get the best measure of the volume of a cracker box: sugar cubes, golf balls, or acorns? Explain.

   _________________________________________________________________
   _________________________________________________________________

**Stretch Your Thinking**

When would you use “about” to describe the volume of a box?
When would you not use “about”?
Measuring Volume in Cubic Centimetres

Quick Review

- The volume of an object is the amount of space inside of it.

A centimetre cube has a volume of one cubic centimetre (1 cm³). We can use centimetre cubes to measure volume.

This box holds 3 rows of 4 cubes, or 12 cubes. The volume of the box is 12 cubic centimetres, or 12 cm³.

- The volume of an object is also the space it occupies. This object has 6 cubes in the bottom layer and 3 cubes in the top layer. The volume is 9 cubic centimetres, or 9 cm³.

Try These

Use centimetre cubes to help.

1. Each prism is made with centimetre cubes. Find the volume of each prism.
   - a) 
   - b) 
   - c) 

2. Order the prisms in question 1 from least to greatest volume. _________
Practice

1. Use centimetre cubes.
   Build 3 different rectangular prisms with a volume of 12 cm$^3$.
   Describe each prism.
   
   a) _____________________________________________________________
   b) _____________________________________________________________
   c) _____________________________________________________________

2. Each object is made with centimetre cubes.
   Estimate the volume of each solid. Then, find each volume.
   a) Estimate: _________
   b) Estimate: _________
   c) Estimate: _________
   
   Volume: ____________ Volume: ____________ Volume: ____________

3. Order the objects in question 2 from greatest to least volume. ___________

4. How many different rectangular prisms with a volume of 11 cm$^3$ can you build with centimetre cubes? Explain.
   _________________________________________________________________
   _________________________________________________________________

Stretch Your Thinking

Find a small box. Estimate its volume in cubic centimetres.
Use centimetre cubes to find the volume of the box.
   a) How did you find the volume of the box?
      _________________________________________________________________
      _________________________________________________________________
   
   b) Is the volume exact or approximate? Explain.
      _________________________________________________________________
      _________________________________________________________________
Constructing Rectangular Prisms with a Given Volume

Quick Review

➤ You can make only 1 rectangular prism using 7 centimetre cubes. The volume of this rectangular prism is 7 cm³.

➤ You can make 4 different rectangular prisms with 16 cubes. The volume of each rectangular prism is 16 cm³.

Try These

1. These rectangular prisms are made with centimetre cubes. Find the volume of each prism.
   a)  
   b)  
   c)  

   ___________________  ___________________  ___________________

2. How many different rectangular prisms can be made with 10 centimetre cubes? _______
   Write the dimensions of each prism.

   ___________________
Practice

1. These rectangular prisms are made with centimetre cubes. Find the volume of each prism.
   a)  
   b)  
   c)  

2. Use centimetre cubes. Build a rectangular prism with each volume. Record your work in the table.
   a) 12 cm$^3$  
   b) 18 cm$^3$  
   c) 11 cm$^3$  
   d) 8 cm$^3$

3. Build a rectangular prism with each set of dimensions. Find the volume of each prism.

4. Vannah built a rectangular prism with 48 centimetre cubes. She put 16 cubes in each layer.
   a) How many layers of cubes does her prism have? _______
   b) What are the dimensions of the prism? Give as many possible answers as you can.

Stretch Your Thinking

Harold built a rectangular prism with 36 centimetre cubes. What might be the dimensions of his prism? Give as many answers as you can.
Measuring Volume in Cubic Metres

Quick Review

A cube with edge lengths of one metre has a volume of one cubic metre (1 m$^3$).

We use cubic metres to measure the volumes of large objects.

This carton is 1 m long, 1 m wide, and 1 m tall. It has a volume of 1 m$^3$.

Twelve of these cartons are stacked in 2 layers of 6. The stack has a volume of 12 m$^3$.

Try These

1. Each rectangular prism is built with 1-m cubes. Find the volume of each prism.

a) __________________ b) __________________ c) __________________

d) __________________ e) __________________ f) __________________

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Practice

1. Name 2 objects whose volume is:
   a) about 1 m$^3$ ___________ ___________
   b) greater than 1 m$^3$ ___________ ___________
   c) less than 1 m$^3$ ___________ ___________

2. Jared and Alyssa made a stack of hay bales. Each bale has a volume of 1 m$^3$. They made 3 layers with 6 bales in each layer.
   a) What is the volume of the stack? _______
   b) How many rows of bales could be in each layer? _______
   c) How many bales could be in each row? _______

3. Which unit would you use to measure the volume of each object: cubic centimetre or cubic metre?
   a) a baby’s playpen ________________
   b) a cake mix box ________________
   c) a storage shed ________________
   d) a transport truck ________________

4. Each rectangular prism is built with 1-m cubes. Find the volume of each prism.
   a) ___________________ ________________
   b) ___________________ ________________
   c) ___________________ ________________

Stretch Your Thinking

A stack of crates has a volume of 48 m$^3$. There are 2 layers in the stack. How many crates long and wide could each layer be? Give as many answers as you can.

__________________________________________

__________________________________________
Exploring Capacity: The Litre

Quick Review

When you measure how much a container holds, you measure its capacity.

This bottle has a capacity of one litre (1 L). The bottle holds 1 L of water.

One litre fills about 4 glasses.

Here are some other things that are measured in litres.

Try These

1. Circle the containers that hold more than one litre.

2. Circle the better estimate.
   a) 4 L or 40 L
   b) 2 L or 20 L
   c) 1 L or 50 L
   d) 2 L or 200 L
Practice

Solve each problem. Show your work.

1. How many litres of milk will it take to fill:
   a) 8 glasses? _______
   b) 16 glasses? _______
   c) 20 glasses? _______
   d) 12 glasses? _______

2. Eva has a 3-L jug of fruit punch.
   How many glasses can she fill? __________

3. Each child at the picnic drank 1 glass of juice.
   There were 18 L of juice served.
   About how many children were at the picnic? _________________

4. Dakota’s family drinks 4 L of milk a day.
   a) How many litres of milk does Dakota’s family drink in a week? _______
   b) How many litres of milk does Dakota’s family drink in the month of April? _______

5. Which containers hold less than 1 L? Which hold more than 1 L?
   a) a mug __________
   b) a baby’s bottle __________
   c) a garbage can __________
   d) a rain barrel __________
   e) a kitchen sink __________
   f) an eyedropper __________

Stretch Your Thinking

Your heart pumps about 5 L of blood a minute.
How many litres of blood does your heart pump in one hour?
"
Exploring Capacity: The Millilitre

Quick Review

The millilitre (mL) is a small unit of capacity. This teaspoon has a capacity of 5 mL.

This measuring cup has a capacity of 500 mL. It holds 500 mL of water.

It takes 2 of these measuring cups to fill a 1-L container.

500 mL + 500 mL = 1000 mL
One litre is equal to one thousand millilitres.
1 L = 1000 mL

Try These

1. Which unit would you use to measure each capacity: millilitre or litre?
   a) b) c)

2. Peter drinks 2 L of water each day. How many millilitres of water does he drink each day?

3. Complete.
   a) 5 L = _____ mL
   b) 2 L = _____ mL
   c) 6 L = _____ mL
   d) 3000 mL = _____ L
   e) 7000 mL = _____ L
   f) 1000 mL = _____ L
Practice

1. Circle the better estimate.
   a) 85 mL or 850 mL  b) 25 mL or 250 mL  c) 15 mL or 500 mL

2. a) Order the capacities of these containers from least to greatest.
   ______________________________________________________________
   b) Which container’s capacity is closest to 1 L? ______________________

3. Which unit would you use to measure each amount: millilitre or litre?
   a) the amount of gasoline in a car __________
   b) the amount of water in a raindrop __________
   c) the amount of nail polish in a bottle __________
   d) the amount of water in a swimming pool __________

4. Hunter bought a 1-L bottle of water. He drank 750 mL of the water.
   How much water does Hunter have left? __________

Stretch Your Thinking

It takes about 30 mL of jam to make a sandwich. About how many sandwiches could you make with this whole jar? ______________
Relating Capacity and Volume

Quick Review

You can find the volume of an object by measuring the amount of water displaced or moved by the object.

There are 250 mL of water in the container.

The prism has raised the water level to 300 mL.

300 mL – 250 mL = 50 mL
The prism displaced 50 mL of water.

1 mL = 1 cm³
50 mL = 50 cm³
So, the volume of the prism is 50 cm³.

Try These

1. What is the volume of each object?
   a) b) c)
Practice

1. You will need a measuring cup marked in millilitres, water, and 6 objects that will sink. Find the volume of each object. Complete the chart.

<table>
<thead>
<tr>
<th>Object</th>
<th>Water Level without Object</th>
<th>Water Level with Object</th>
<th>Amount of Water Displaced</th>
<th>Volume of the Object</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
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</tbody>
</table>

2. Order the objects you used in question 1 from least to greatest volume.

-------------------------------------------------------------------------------------------------

Stretch Your Thinking

Nancy filled a measuring cup with water to the 450-mL mark. She dropped 4 golf balls into the cup. The water level rose to the 650-mL mark. What is the volume of one golf ball? Explain.

__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
__________________________________________________________________
Equivalent Fractions

Quick Review

- $\frac{1}{3}$ of the circle is shaded.
- $\frac{2}{6}$ of the circle is shaded.
- $\frac{3}{9}$ of the circle is shaded.
- $\frac{4}{12}$ of the circle is shaded.

- $\frac{1}{3}$, $\frac{2}{6}$, $\frac{3}{9}$, and $\frac{4}{12}$ name the same amount. They are equivalent fractions.

- There are patterns in the equivalent fractions.
  - The numerators are multiples of the least numerator, 1.
  - The denominators are multiples of the least denominator, 3.

- You can multiply or divide the numerator and the denominator of a fraction by the same number to find equivalent fractions.

Try These

Write 3 equivalent fractions for each picture.

1. 

2. 

3. 

68
Practice

1. Write 2 equivalent fractions for each fraction. Use the diagram to help.

   a) \( \frac{1}{4} \) __________  
   b) \( \frac{2}{4} \) __________  
   c) \( \frac{3}{4} \) __________  
   d) \( \frac{4}{4} \) __________

2. Write as many equivalent fractions as you can for each picture.
   a) 
   
   b) 
   
   c) 

3. Draw a picture to show each pair of equivalent fractions.
   a) \( \frac{2}{5} \) and \( \frac{6}{15} \)  
   b) \( \frac{4}{6} \) and \( \frac{16}{24} \)

Stretch Your Thinking

Find as many equivalent fractions as you can for the shaded section of this hundredths grid.
Comparing and Ordering Fractions

Quick Review

Here are some ways to compare and order fractions.

➢ To order \(\frac{1}{2}, \frac{4}{5}\), and \(\frac{2}{3}\):
  1. Draw a number line.
  2. Divide, mark, and label the number line.
  3. From least to greatest: \(\frac{1}{2}, \frac{2}{3}, \frac{4}{5}\)

➢ To compare \(\frac{4}{5}\) and \(\frac{3}{4}\):
  1. List equivalent fractions until the numerators or denominators are the same.
  2. \(\frac{4}{5} = \frac{8}{10} = \frac{12}{15} = \frac{16}{20} = \frac{20}{25}\)
  3. \(\frac{3}{4} = \frac{6}{8} = \frac{9}{12} = \frac{12}{16} = \frac{15}{20}\)
  4. Since \(\frac{12}{15} > \frac{12}{16}\), then \(\frac{4}{5} > \frac{3}{4}\)
  5. or, since \(\frac{16}{20} > \frac{15}{20}\), then \(\frac{4}{5} > \frac{3}{4}\).

Try These

1. a) Show thirds, fourths, and sixths on a number line.

   ![Number Line]

   \[0\quad 0.5\quad 1\]

   b) Use the number line above to order these fractions from least to greatest:

   \(\frac{2}{3}, \frac{3}{4}, \frac{2}{6}\)

   ____________

2. Use equivalent fractions to compare the fractions in each pair.
   a) \(\frac{4}{5}\) and \(\frac{9}{10}\)

   ________________

   b) \(\frac{2}{3}\) and \(\frac{5}{8}\)

   ________________
Practice

1. Use the strips below to order these fractions from least to greatest: \( \frac{3}{4}, \frac{5}{6}, \frac{5}{8} \)

2. Use equivalent fractions to compare the fractions in each pair. Write >, <, or =.
   a) \( \frac{3}{4} \underline{\quad} \frac{7}{8} \)
   b) \( \frac{1}{2} \underline{\quad} \frac{3}{7} \)
   c) \( \frac{2}{3} \underline{\quad} \frac{5}{9} \)
   d) \( \frac{3}{5} \underline{\quad} \frac{2}{10} \)

3. Which fraction in each pair is greater? Tell how you know.
   a) \( \frac{3}{8} \underline{\quad} \frac{5}{8} \)
   b) \( \frac{4}{5} \underline{\quad} \frac{4}{7} \)
   c) \( \frac{6}{12} \underline{\quad} \frac{7}{24} \)

4. Name 4 fractions that are less than \( \frac{2}{3} \).
   Each fraction should have a different denominator.

Stretch Your Thinking

1. Write a fraction to make each statement true.
   a) \( \frac{7}{8} < \underline{\quad} \)
   b) \( \frac{99}{100} > \underline{\quad} \)
   c) \( \underline{\quad} < \frac{1}{4} \)
   d) \( \underline{\quad} > \frac{1}{8} \)
Relating Fractions to Decimals

Quick Review

► You can write fractions with denominators of 10 and 100 as decimals.

\[ \frac{6}{10} \text{ is 6 tenths or } 0.6. \quad \frac{9}{100} \text{ is 9 hundredths or } 0.09. \]

► If a fraction does not have a denominator of 10 or 100, try to find an equivalent fraction that does.

\[ \frac{1}{5} \text{ is equivalent to } \frac{2}{10}. \]
\[ \frac{2}{10} \text{ is 2 tenths, or 0.2.} \]
\[ \frac{1}{5} \text{ and 0.2 are equivalent.} \]

\[ \frac{1}{4} \text{ is equivalent to } \frac{25}{100}. \]
\[ \frac{25}{100} \text{ is 25 hundredths or 0.25.} \]
\[ \frac{1}{4} \text{ and 0.25 are equivalent.} \]

Try These

1. Write a fraction and a decimal to describe the shaded part of each grid.
   a) [Grid Image]
   b) [Grid Image]
   c) [Grid Image]
Practice

1. Colour each grid to show the fraction. Then, write the fraction as a decimal.
   a)  
   b)  
   c)  

   \[ \frac{3}{4} \quad \frac{8}{100} \quad \frac{3}{5} \]

2. Use >, <, or = to make each statement true.
   a) \[ \frac{1}{4} \quad \frac{25}{100} \]  
   b) \[ 0.07 \quad \frac{2}{100} \]  
   c) \[ 0.2 \quad \frac{20}{100} \]  
   d) \[ \frac{3}{5} \quad \frac{30}{100} \]  
   e) \[ \frac{3}{4} \quad \frac{95}{100} \]  
   f) \[ \frac{1}{2} \quad 0.5 \]

3. Write an equivalent fraction for each decimal.
   a) 0.25  
   b) 0.4  
   c) 0.6  
   d) 0.75  

4. Write each fraction as a decimal.
   a) \[ \frac{1}{2} \]  
   b) \[ \frac{16}{20} \]  
   c) \[ \frac{3}{5} \]  
   d) \[ \frac{36}{100} \]  
   e) \[ \frac{3}{4} \]  
   f) \[ \frac{4}{5} \]

Stretch Your Thinking

Write a decimal that is close in value to each of these fractions:
\[ \frac{1}{3} \quad \frac{2}{3} \]  
\[ \frac{1}{8} \quad \frac{5}{8} \]
Fraction and Decimal Benchmarks

Quick Review

You can use benchmarks to compare and order decimals.

Order 0.8, 0.42 and 0.31 from least to greatest.

Use equivalent decimals.

0.0 = 0.00 0.5 = 0.50 0.8 = 0.80 1.0 = 1.00

0.31 and 0.42 are between 0.00 and 0.50.
0.31 < 0.42
0.80 is between 0.50 and 1.00

From least to greatest: 0.31, 0.42, 0.8

Try These

1. Estimate to place the decimals on the number line. Order the decimals from least to greatest.

   a) 0.30, 0.10, 0.70

   From least to greatest: ____________________________

   b) 0.65, 0.6, 0.2

   From least to greatest: ____________________________
Practice

1. Complete. Use >, <, or =.
   a) 0.40 _____ 0.70  
   b) 0.25 _____ 0.17  
   c) 0.7 _____ 0.70  
   d) 0.48 _____ 0.4  
   e) 0.90 _____ 0.9  
   f) 1.0 _____ 0.99  

2. Order the decimals in each set from greatest to least.
   a) 0.6, 0.24, 0.12  ______________
   b) 0.8, 0.75, 0.3     ______________
   c) 0.14, 0.2, 0.35  ______________
   d) 0.92, 0.1, 0.11  ______________

3. a) Complete the table.
   b) Order the decimals in the table from least to greatest.

<table>
<thead>
<tr>
<th>Decimal</th>
<th>Lower Benchmark</th>
<th>Upper Benchmark</th>
<th>Nearest Benchmark</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.19</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.40</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.86</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>0.07</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

4. Use the number line below to compare the numbers \( \frac{3}{4} \) and 0.7.

   ______________

5. Manny’s snail travelled 0.89 m in 10 min. Bertha’s snail travelled 0.9 m in 10 min. Whose snail travelled the greater distance?

   ______________

Stretch Your Thinking

Order these numbers from least to greatest:
0.23, \( \frac{7}{10} \), 0.04, \( \frac{3}{4} \), 0.8

   ______________
Exploring Thousandths

Quick Review

Numbers with **thousandths** can be shown in different ways.

We can write some fractions with denominator 1000.

\[
\frac{1}{4} \text{ is equivalent to } \frac{250}{1000}.
\]

So, \( \frac{1}{4} \) is equivalent to 0.250.

We can write decimals in expanded form.

\[4.623 = 4 \text{ ones} + 6 \text{ tenths} + 2 \text{ hundredths} + 3 \text{ thousandths} = 4 + 0.6 + 0.02 + 0.003\]

0.700, 0.70, and 0.7 name the same amount.
They are **equivalent decimals**.

Try These

1. Write each number as a decimal.
   a) \( \frac{7}{100} \)  
   b) \( \frac{14}{1000} \)  
   c) \( \frac{19}{100} \)  
   d) \( \frac{6}{1000} \)  
   e) \( \frac{374}{1000} \)  
   f) \( \frac{108}{1000} \)

2. Write each decimal in expanded form.
   a) 0.405
   b) 84.037

3. Write an equivalent decimal for each decimal.
   a) 0.23  
   b) 0.6
Practice

1. Record each number in the place-value chart.
   a) 76 thousandths
   b) 316 and 536 thousandths
   c) 185 thousandths
   d) 93 and 3 thousandths

<table>
<thead>
<tr>
<th></th>
<th>Hundreds</th>
<th>Tens</th>
<th>Ones</th>
<th>Tenths</th>
<th>Hundredths</th>
<th>Thousandths</th>
</tr>
</thead>
<tbody>
<tr>
<td>a)</td>
<td></td>
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</tr>
<tr>
<td>b)</td>
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<td>c)</td>
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<td>d)</td>
<td></td>
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</tr>
</tbody>
</table>

2. Write each number as a fraction.
   a) 0.047 __________
   b) 0.354 __________
   c) 0.739 __________
   d) 0.001 __________
   e) 0.72 ___________  
   f) 0.506 __________

3. Write each number in question 2 in expanded form.
   a) ______________________
   b) ______________________
   c) ______________________
   d) ______________________
   e) ______________________
   f) ______________________

4. Write each fraction as a decimal.
   a) \( \frac{9}{1000} \) __________
   b) \( \frac{6}{100} \) ____________
   c) \( \frac{85}{1000} \) ____________
   d) \( \frac{25}{1000} \) ____________
   e) \( \frac{367}{1000} \) ____________
   f) \( \frac{8}{1000} \) ____________

Stretch Your Thinking

Use the digits 0, 2, 3, and 6.
Make a number that is greater than 1 but less than 4.
Find as many numbers as you can.

_________________________________________________________________
_________________________________________________________________
Comparing and Ordering Decimals

Quick Review

The table shows the masses of Henry’s 3 kittens.

Here are 2 ways to order the pets from least to greatest mass.

➤ Use a place-value chart.

<table>
<thead>
<tr>
<th>Kitten</th>
<th>Mass (kg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Foofoo</td>
<td>0.395</td>
</tr>
<tr>
<td>Quigley</td>
<td>0.364</td>
</tr>
<tr>
<td>Oscar</td>
<td>0.391</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Ones</th>
<th>Tenths</th>
<th>Hundredths</th>
<th>Thousandths</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>3</td>
<td>9</td>
<td>5</td>
</tr>
<tr>
<td>0</td>
<td>3</td>
<td>6</td>
<td>4</td>
</tr>
<tr>
<td>0</td>
<td>3</td>
<td>9</td>
<td>1</td>
</tr>
</tbody>
</table>

All 3 numbers have 0 ones and 3 tenths.
0.364 has the least number of hundredths, so it is the least number.
0.395 has the greatest number of thousandths, so it is the greatest.

The pets in order from least to greatest mass are: Quigley, Oscar, Foofoo.

➤ Use a number line.

Reading numbers from left to right gives the masses from least to greatest.

Try These

1. Use $>$, $<$, or $=$ to make each statement true.
   a) $0.457 \quad \quad 0.406$
   b) $17.63 \quad \quad 17.630$
   c) $5.976 \quad \quad 6.0$

2. Order the numbers from greatest to least.
   a) $0.36, 0.371, 0.329$
   b) $2.76, 5.3, 2.485$
Practice

1. Play this game with a partner.
   You will need 2 sets of 10 cards numbered 0 to 9, in a paper bag.
   ➤ Take turns drawing a card from the bag.
   Record the digit in any space in the first row of your game board.
   Return the card to the bag.
   ➤ Continue until all 4 spaces in a row are filled.
   ➤ Compare your numbers using $>$ or $<$.
   ➤ The player with the greater number wins a point.
   ➤ Play 4 more rounds.
   The player with the higher score wins.

<table>
<thead>
<tr>
<th>Player A</th>
<th>Player B</th>
</tr>
</thead>
<tbody>
<tr>
<td>_____ . _____ . _____ . _____</td>
<td>□ . _____ . _____ . _____</td>
</tr>
<tr>
<td>_____ . _____ . _____ . _____</td>
<td>□ . _____ . _____ . _____</td>
</tr>
<tr>
<td>_____ . _____ . _____ . _____</td>
<td>□ . _____ . _____ . _____</td>
</tr>
<tr>
<td>_____ . _____ . _____ . _____</td>
<td>□ . _____ . _____ . _____</td>
</tr>
</tbody>
</table>

2. a) Write your numbers from the game in order from greatest to least.

   __________________________________________________________

b) Write your partner’s numbers from the game in order from least to greatest.

   __________________________________________________________

Stretch Your Thinking

Write all the numbers from the game in order from least to greatest.

   __________________________________________________________
Quick Review

There are relationships among the units you use to measure length.  
You can read the length of this shoe in several ways.

The shoe is 17 cm long.
Since 1 cm is 10 mm, then 17 cm is 170 mm.
The shoe is 170 mm long.
Since 1 cm is 0.01 m, then 17 cm is 0.17 m.
The shoe is 0.17 m long.

1 mm = 0.1 cm  1 cm = 10 mm  1 m = 1000 mm
1 mm = 0.001 m 1 cm = 0.01 m  1 m = 100 cm

Try These

1. Record each measure in millimetres and metres.
   a) 7 cm ______________________  b) 56 cm ______________________
   c) 13 cm ______________________ d) 40 cm ______________________

2. Record each measure in millimetres and centimetres.
   a) 4 m ________________________ b) 6 m _________________________
   c) 3.2 m ________________________ d) 40 m _________________________

3. Use =, <, or > to make each statement true.
   a) 4.16 m ____ 416 cm  
   b) 75 cm ____ 7.5 m
   c) 7.2 m ____ 7200 mm
Practice

1. Complete.
   a) 53 cm = ______ m  
   b) 4.1 m = ______ cm 
   c) 85 mm = ______ cm 
   d) 0.25 m = ______ cm 
   e) 8.6 m = _____ mm 
   f) 25 cm = _____ mm 

2. Write each length using 2 different units.
   a) 60 mm _____________________ 
   b) 4 cm _____________________ 
   c) 0.03 m _____________________ 
   d) 2.5 m _____________________ 

3. Here are the lengths of 5 types of eggs.
   a) Which is longer, a robin egg or a cuckoo egg? ________________ 
   b) Which is shorter, a hummingbird egg or a robin egg? ________________ 
   c) About how many times as long as a Canada goose egg is an ostrich egg? ______ 
   d) Put the eggs in order from shortest to longest. 

4. Darwin is 1.06 m tall. Carleton is 157 cm tall.
   Which boy is taller? ________________  How much taller is he? ________ 

5. Draw a line 9 cm long. Write its length using 2 other units. 

Stretch Your Thinking

Which would you rather have, a pile of loonies 350 mm tall or a pile of loonies 0.49 m tall? Explain.
Relating Fractions and Decimals to Division

Quick Review

➤ Wayne has 5 fruit bars to share among 3 people. How much will each person get?

Divide.

Five fruit bars shared among 3 people is written as $5 \div 3 = \frac{1 \text{ R}2}{3\frac{1}{3}}$.

There are 2 left over.

Divide each leftover fruit bar in thirds.

There are 6 thirds.

Each person gets 2 thirds of the leftover fruit bars.

So, each person gets 1 fruit bar and $\frac{2}{3}$ more.

➤ Any division statement can be written as a fraction.

$5 \div 3 = \frac{5}{3}$

Try These

1. Write each division statement as a fraction.
   a) $3 \div 7$ ________
   b) $4 \div 6$ ________
   c) $5 \div 9$ ________
   d) $8 \div 6$ ________
   e) $10 \div 4$ ________
   f) $12 \div 5$ ________

2. Write each fraction as a division statement.
   a) $\frac{4}{5}$ ________
   b) $\frac{12}{8}$ ________
   c) $\frac{15}{4}$ ________
   d) $\frac{1}{6}$ ________
   e) $\frac{3}{4}$ ________
   f) $\frac{26}{3}$ ________
Practice

Draw a picture to solve each problem. Show all your work.

1. How many pears would each person get if 14 pears are shared among 4 people?

2. Salvador baked 3 apple tarts.
   He shared them equally among 4 friends.
   How much did each friend get?

3. Eight people won $200. How much will each person’s share be?

Stretch Your Thinking

Each of 4 people got 5 cookies and \( \frac{3}{4} \) more.
How many cookies were shared?
Quick Review

Here are 2 ways to estimate $4.548 + 2.417$.

➤ Write each decimal to the nearest whole number:
  $5 + 2 = 7$  So, $4.548 + 2.417$ is about $7$.

➤ Write only 1 decimal to the nearest whole number:
  $5 + 2.417 = 7.417$  So, $4.548 + 2.417$ is about $7.417$.

Here are 2 ways to estimate $4.538 - 2.417$.

➤ Write the second decimal to the nearest whole number:
  $4.538 - 2 = 2.538$  So, $4.538 - 2.417$ is about $2.538$.

➤ Write both decimals to the nearest whole number:
  $5 - 2 = 3$
  So, $4.538 - 2.417$ is about $3$.

Try These

1. Estimate each sum.

   a) $2.54 + 7.16$
   
   b) $4.197 + 3.864$
   
   c) $0.765 + 1.295$

   d) $5.765 + 3.189$
   
   e) $0.473 + 1.697$
   
   f) $2.008 + 3.801$

2. Estimate each difference.

   a) $7.546 - 3.518$
   
   b) $2.476 - 1.555$
   
   c) $7.9 - 3.267$

   d) $3.204 - 0.938$
   
   e) $1.497 - 0.126$
   
   f) $12.094 - 8.259$
Practice

1. Estimate each sum or difference.
   a) \(27.6 + 49.23\)  
b) \(16.257 - 9.396\)  
c) \(4.875 - 2.93\)  
d) \(7.596 + 2.17\)  
e) \(13.123 - 6.959\)  
f) \(10.67 + 7.834\)

2. a) Joline bought a pair of skates for $79.95. She also bought a pullover for $45.25.  
    Estimate the total cost of Joline's purchases. 
    b) Estimate how much more Joline paid for the skates than the pullover.

3. The table shows the masses of five puppies.
   a) Estimate the combined masses of:
      Brutus and Zeus 
      Tawny and Zena 
      Zeus and Zara 
      Zara and Tawny 
   b) Estimate the difference in masses of:
      Zara and Zena 
      Brutus and Zeus 
      Tawny and Zara 
      The heaviest and lightest puppies 

4. Circle the better estimate.
   a) \(3.549 + 6.831\)  9 or 10  
b) \(4.316 - 0.135\)  3 or 4

Stretch Your Thinking

Estimate the combined mass of the five puppies.
Adding Decimals

Quick Review

Madison rode her bike 11.76 km on Saturday and 6.18 km on Sunday. What total distance did Madison ride?

You can use place value to add 11.76 + 6.18.

First estimate. 11.76 is about 12. 6.18 is about 6.

12 + 6 = 18

Step 1: Record the numbers. Align them as they are aligned in the place-value chart.

11.76
+ 6.18

Step 2: Add as you would with whole numbers.

11.76
+ 6.18
17.94

17.94 is close to the estimate of 18, so the answer is reasonable.

Try These

1. Estimate first. Then add.

   a) 3.4 + 9.3
   b) 6.8 + 4.7
   c) 7.54 + 3.62
   d) $8.09 + 7.68

   e) 25.2 + 13.9
   f) $43.16 + $8.97
   g) 0.97 + 1.23
   h) 18.40 + 26.60
Practice

1. Add. Estimate to check.
   a) 9.7 + 4.9
   b) 16.3 + 12.8
   c) $4.07 + $8.63
   d) 21.60 + 14.73
   e) 35.7 + 98.6
   f) $1.54 + $3.65
   g) 6.28 + 12.32
   h) 47.37 + 19.08

2. Play this game with a partner.
   You will need paper, pencils, and a number cube, labelled 1 to 6.
   The object of the game is to get the greater sum.
   ➤ Draw an addition grid like this on your paper:

   +

   ➤ Take turns to roll the number cube. Record the number rolled in any box in your addition grid.
   ➤ Continue until all the boxes in your grid are full.
   ➤ Add. The player with the greater sum scores 1 point.
   ➤ Play 4 more rounds to find the overall winner.
   ➤ Play the game again. This time, try to get the lesser sum.

Stretch Your Thinking

Find 2 decimals with a sum of 9.76.
Do this in as many ways as you can.
Quick Review

Joline grew 2 pumpkins in her garden. The masses of her pumpkins are 7.05 kg and 9.84 kg. What is the difference in the masses?

You can use place value to find 9.84 – 7.05.

Step 1: Record the numbers. Align them as they are aligned in the place-value chart.

<table>
<thead>
<tr>
<th>Ones</th>
<th>Tenths</th>
<th>Hundredths</th>
</tr>
</thead>
<tbody>
<tr>
<td>9</td>
<td>8</td>
<td>4</td>
</tr>
<tr>
<td>7</td>
<td>0</td>
<td>5</td>
</tr>
</tbody>
</table>

9.84
– 7.05

Step 2: Subtract as you would with whole numbers.

9.84
– 7.05
2.79

Add to check your answer.

7.05
+ 2.79
9.84

Try These

1. Estimate first. Then subtract.
   a) 6.8
   b) 8.5
   c) 2.67
   d) $12.45
      – 4.3
      – 0.9
      – 1.38
      – $ 8.68
Practice

1. Subtract. Add to check.
   a) 9.4  
   b) 25.8  
   c) 7.04  
   d) 8.62  
   - 6.8  
   - 16.9  
   - 2.13  
   - 5.74  
   e) 14.25  
   f) $20.15  
   g) 84.08  
   h) 52.34  
   - 8.37  
   - $9.48  
   - 47.16  
   - 26.89

2.  
   a) How much more than the jacket do the jeans cost? __________________
   b) Jerry paid for a baseball hat with a $10 bill. How much change did he get? __________________________________
   c) Sylvie bought a shirt and a pair of socks. She gave the clerk $20. How much change did she get? __________________________________
   d) What is the difference in price between the least expensive and most expensive items? ______________________________________________
   e) Which 2 items have each difference in price?
      $26.30 ____________________________________________________
      $15.10 ____________________________________________________
      $6.76 ____________________________________________________

Stretch Your Thinking

Name 2 decimals whose difference is between 9 and 10, but closer to 9.
You can use place value to add 5.763 and 3.949.

**Step 1:** Estimate.

Write the second decimal to the nearest whole number.

So, 5.763 + 3.949 is about 9.763.

9.712 is close to the estimate, so the answer is reasonable.

You can use place value to subtract 3.949 from 5.763.

**Step 1:** Subtract as you would with whole numbers.

So, 5.763 − 4 = 1.763

1.814 is close to the estimate, so the answer is reasonable.

**Try These**

1. **Add. Estimate to check your answers.**
   
   a) 4.521 + 3.097
   
   b) 2.168 + 0.948
   
   c) 7.169 + 8.473
   
   d) 6.704 + 0.491

2. **Subtract. Estimate first. Then subtract.**
   
   a) 9.732 − 0.489
   
   b) 6.371 − 1.098
   
   c) 4.152 − 4.097
   
   d) 3.652 − 1.984
Practice

1. Add. Use subtraction to check each answer.
   
   a) \[4.157 + 6.346 = 10.497\]  
   b) \[27.309 + 14.167 = 41.476\]  
   c) \[3.187 + 4.679 = 7.866\]  
   d) \[5.138 + 12.349 = 17.487\]  
   e) \[0.573 + 4.497 = 5.069\]  
   f) \[36.234 + 14.875 = 51.109\]

2. Subtract. Use addition to check each answer.
   
   a) \[7.243 - 2.807 = 4.436\]  
   b) \[4.583 - 2.338 = 2.245\]  
   c) \[13.040 - 7.862 = 5.178\]  
   d) \[11.431 - 8.763 = 2.668\]  
   e) \[4.010 - 2.862 = 1.148\]  
   f) \[73.832 - 51.765 = 22.067\]

3. The difference in the masses of 2 objects is 0.479 kg.
   
   a) What might the mass of each object be? ________________
   
   b) What might the objects be? ________________

4. Salvatore ran 2.457 km on Saturday and 3.169 km on Sunday.
   
   a) How far did Salvatore run in all? ________________
   
   b) How much further did he run on Sunday than on Saturday? ________________

Stretch Your Thinking

Use each of the digits 1 to 8 once to make this subtraction true.

\[\square . \square \square \square \square - \square . \square \square \square = 1.347\]
Here are some attributes of shapes.

➤ The lengths of the sides:

This shape has some sides the same length. This shape has all sides the same length.

➤ The direction of the sides:

This shape has 2 pairs of parallel sides. This shape has no parallel sides.

➤ We can label each vertex and then name the shape by its vertices.

This is triangle JKL. It has 3 sides: JK, JL, and KL

Try These

1. Tell which shapes have:
   a) no parallel sides _______
   b) all sides different lengths _______
   c) all sides the same length _______
   d) some parallel sides _______

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Practice

1. Find the shapes below that have each of these attributes. Label the shapes with the letters.

   A — has all sides the same length
   B — has no sides the same length
   C — has some sides the same length
   D — has 1 pair of parallel sides
   E — has 2 pairs of parallel sides
   F — has more than 2 pairs of parallel sides
   G — has no parallel sides

2. a) Use letters to name this shape. _______
   b) Use letters to name the sides. _____________

Stretch Your Thinking

Draw as many figures as you can with 2 pairs of parallel sides.
Quick Review

➤ Look at the chalkboard.

The top and bottom edges are horizontal. The side edges are vertical. A horizontal edge and a vertical edge are perpendicular. That is, these edges intersect to form a right angle.

When 2 sides of any shape make a right angle, we say the sides are perpendicular. We draw a square to show a right angle.

This shape has 5 sides. It is a pentagon. In pentagon ABCDE, BC is perpendicular to CD. We write: BC \( \perp \) CD. Also, ED \( \perp \) CD.

Try These

1. Tell which shapes have:
   a) three right angles ______
   b) no right angles ______
   c) one right angle ______

2. Look at the shape. Name:
   a) horizontal sides ______
   b) vertical sides ______
   c) perpendicular sides ________________________
Practice

1. Use the dot paper below.
   Draw a shape that fits each description.
   Label each shape with its letter.

   A — has exactly four right angles
   B — has only one right angle
   C — has exactly 2 pairs of perpendicular sides
   D — has no right angles
   E — has exactly 3 horizontal sides
   F — has exactly 1 pair of perpendicular sides

---

Stretch Your Thinking

Draw a shape on the dot paper.
Give your shape as many right angles as you can.
Quick Review

- A square has 4 sides equal. The diagonals are equal and perpendicular.

- A rectangle has 2 pairs of opposite sides equal. The diagonals are equal.

- A rhombus has 4 sides equal. The diagonals are perpendicular.

- A parallelogram has 2 pairs of opposite sides equal.

- All squares, rectangles, parallelograms, and rhombuses have 2 pairs of parallel sides.

- A trapezoid has exactly 1 pair of parallel sides.

- A kite has exactly 2 pairs of equal adjacent sides.

Try These

1. Draw 2 different quadrilaterals on the dot paper. Mark equal sides with hatch marks. Mark parallel sides with arrows.
Practice

1. Play this game with a partner.
   You will need:
   - Dot paper
   - Pencil

   Player A
   ➤ Make a quadrilateral on the dot paper without letting your partner see.
   The quadrilateral should have at least one pair of equal or parallel sides.

   Player B
   ➤ Ask your partner “Yes–No” questions about the quadrilateral.
   The questions can be about
   - the number of equal sides
   - the number of parallel sides
   - the diagonals
   ➤ Keep asking questions until you think you know the quadrilateral.
   Guess the quadrilateral. If you are right, you get a point.
   Switch roles and play again.
   Keep playing until one player has 5 points.

Stretch Your Thinking

Explain why this quadrilateral cannot be called a square, a parallelogram, a rectangle, a rhombus, or a trapezoid.
Other Attributes of Quadrilaterals

Quick Review

All squares and rectangles have 4 right angles. Adjacent sides are perpendicular.

A shape is symmetrical when it can be folded so that one part matches the other part exactly. The fold line is the line of symmetry.

- No lines of symmetry
- 1 line of symmetry
- 2 lines of symmetry
- 4 lines of symmetry

Try These

1. Draw a quadrilateral with each attribute.
   a) 0 lines of symmetry  b) 1 line of symmetry  c) exactly 2 right angles

2. Why is a rectangle not a kite?

98
1. Use the Venn diagram to sort the quadrilaterals.

2. a) Draw a trapezoid on the dot grid.
   b) Write a statement about your trapezoid that is true.
      _________________________________
      _________________________________
   c) Write a statement about a trapezoid that is never true.
      _________________________________
      _________________________________

Stretch Your Thinking

Explain why a square is a parallelogram and a rhombus.

_______________________________
_______________________________
_______________________________
Exploring Faces and Edges of Objects

Quick Review

The rectangular prism sits on a table. Look at its edges. The bold edges are horizontal. The longer edges are parallel. The shorter edges are parallel. Each other edge is perpendicular to the edges where the bold edges intersect.

Here is the same prism. Look at its faces. The shaded faces are horizontal. They are also parallel. Each unshaded face is vertical. So, each unshaded face is perpendicular to the shaded faces. The two pairs of opposite unshaded faces are also parallel.

Try These

1.

A
B
C
D

Write the letters of the objects that have:

a) horizontal edges ________  b) horizontal faces ________
c) perpendicular edges ________  d) vertical faces ________
e) parallel edges ________  f) parallel faces ________
Practice

1. a) How are these prisms the same?
   ____________________________________
   ____________________________________
   ____________________________________

   b) How are they different?
   _____________________________________
   _____________________________________

2. Write the letters of the objects that have:
   a) parallel edges ______
   b) parallel faces _____
   c) perpendicular edges _____
   d) perpendicular faces _____
   e) vertical edges _____
   f) vertical faces _____

3. Look at this object.
   Write how many of each:
   a) parallel faces ______
   b) horizontal edges ______
   c) horizontal faces ______
   d) vertical faces ______

Stretch Your Thinking

Find a geometric object. Write a riddle that describes the attributes of the object.
Ask a classmate to solve your riddle.

___________________________________________________________________
___________________________________________________________________
Quick Review

Here is how to draw a triangular prism on triangular dot paper:

Step 1

Step 2

Step 3

Here is how to draw a rectangular prism on square dot paper:

Step 1

Step 2

Step 3

Try These

Follow the steps above to draw:

a) the triangular prism

b) the rectangular prism
Practice

1. Each picture below is the front or back face of a prism.
   Complete each prism.
   a) 
   b) 

2. Each picture below is the base of a pyramid.
   Complete each pyramid.
   a) 
   b) 

3. Draw a prism with a pentagonal front face.

Stretch Your Thinking

Draw as many prisms as you can that have a square as a front face.
First-Hand Data and Second-Hand Data

Quick Review
Data that you collect yourself are called first-hand data.
Data collected by someone else are called second-hand data.

➤ Kriti read the temperature outside the classroom window every day for a week. For Kriti, these results are first-hand data. For you, these results are second-hand data.

➤ Kriti also looked at temperatures in the newspaper. These results are second-hand data.

<table>
<thead>
<tr>
<th>Day</th>
<th>Temperature (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Monday</td>
<td>5</td>
</tr>
<tr>
<td>Tuesday</td>
<td>8</td>
</tr>
<tr>
<td>Wednesday</td>
<td>7</td>
</tr>
<tr>
<td>Thursday</td>
<td>9</td>
</tr>
<tr>
<td>Friday</td>
<td>11</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>City</th>
<th>Temperature (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Acapulco</td>
<td>32</td>
</tr>
<tr>
<td>Cairo</td>
<td>24</td>
</tr>
<tr>
<td>Tokyo</td>
<td>14</td>
</tr>
<tr>
<td>Bangkok</td>
<td>33</td>
</tr>
</tbody>
</table>

Try These

1. Would you use first-hand or second-hand data to answer each question?

   a) How many students in your class wear glasses? ________________
   
   b) Which foods are high in fibre? ____________________________
   
   c) What is the population of China? ___________________________
   
   d) What are the favourite sports of students in your class? __________
   
   e) How many people visit the Yukon each year? ________________

2. Charlie wants to find out how many birds come to the feeder in his backyard each day. Should he use first-hand or second-hand data? Explain.

   __________________________
   __________________________
Practice

1. Rae-Lyn wonders how many children on her street take the bus to school. She counts the children as they get on the bus. Are these first-hand or second-hand data? Explain.

2. Miroki uses a Statistics Canada Web site to find the population of the capital city of each province and territory. Are these first-hand or second-hand data? Explain.

3. Would you use first-hand or second-hand data to answer each question?
   a) How many planets have rings?
   b) How much water do your classmates drink in a day?
   c) How many new vehicles are sold in Canada each year?

4. Name 3 different sources you could go to for second-hand data.

5. Mariya wants to find out how many lighthouses there are in Canada. Should she use first-hand or second-hand data? Why?

Stretch Your Thinking

Name 3 questions you could answer by using second-hand data.
Interpreting Double Bar Graphs

Quick Review

A double bar graph displays two sets of data at once.

The vertical axis shows the places to visit.
The horizontal axis shows how many students want to visit each place.
The scale is one square represents 1 student.
The legend tells what the 2 colours represent.

From the double bar graph, we know that:
• More boys than girls want to go to the planetarium.
• More girls than boys want to go to the art gallery.

Try These

Use the double bar graph above to answer these questions.

1. What is the most popular choice for boys? __________________________
   For girls? __________________________
2. How many boys were surveyed? _____  How many girls? _____
3. What is the least popular choice for boys? __________________________
   For girls? __________________________
Practice

1. For the first graph above:
   a) Write a question you could answer using the graph.
      ______________________________________________________________
   b) Answer your question. _________________________________________
      ______________________________________________________________

2. For the second graph above:
   a) Write a question you could answer using the graph.
      ______________________________________________________________
   b) Answer your question. _________________________________________
      ______________________________________________________________

Stretch Your Thinking

What could this double bar graph represent?
Give the graph a title and legend.
Label each axis.

____________________________________
____________________________________
____________________________________
____________________________________
# Constructing Double Bar Graphs

## Quick Review

This table shows the results of a survey. You can display these data in a double bar graph.

<table>
<thead>
<tr>
<th>Subject</th>
<th>Girls</th>
<th>Boys</th>
</tr>
</thead>
<tbody>
<tr>
<td>Math</td>
<td>24</td>
<td>22</td>
</tr>
<tr>
<td>Science</td>
<td>30</td>
<td>33</td>
</tr>
<tr>
<td>Language Arts</td>
<td>18</td>
<td>16</td>
</tr>
<tr>
<td>Social Studies</td>
<td>14</td>
<td>12</td>
</tr>
</tbody>
</table>

1. First, draw and label 2 axes. Then choose a scale.
2. Draw 2 bars for each subject in the table.
3. Finally, draw a legend and give the graph a title.

## Try These

1. Draw a double bar graph to display the data in the table.

<table>
<thead>
<tr>
<th>Type of Tree</th>
<th>May</th>
<th>June</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maple</td>
<td>200</td>
<td>175</td>
</tr>
<tr>
<td>Elm</td>
<td>125</td>
<td>120</td>
</tr>
<tr>
<td>Oak</td>
<td>175</td>
<td>200</td>
</tr>
</tbody>
</table>

2. Write a question about the graph. Answer the question.
Practice

1. a) Draw a double bar graph to display the data in the table.

Rolling a Number Cube

<table>
<thead>
<tr>
<th>Number Rolled</th>
<th>Ali</th>
<th>Yashi</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>###</td>
<td>III</td>
</tr>
<tr>
<td>2</td>
<td>I###</td>
<td>###</td>
</tr>
<tr>
<td>3</td>
<td>II###</td>
<td>### I</td>
</tr>
<tr>
<td>4</td>
<td>###</td>
<td>III</td>
</tr>
<tr>
<td>5</td>
<td>###</td>
<td>### I</td>
</tr>
<tr>
<td>6</td>
<td>###</td>
<td>### I</td>
</tr>
</tbody>
</table>

b) How many rolls did each person make? __________

c) Which number came up most often? __________

d) What conclusions can you draw from the graph?

Stretch Your Thinking

Draw a graph to display the data in this table.

Olympic Medals Won

<table>
<thead>
<tr>
<th>Athlete</th>
<th>Gold</th>
<th>Silver</th>
<th>Bronze</th>
</tr>
</thead>
<tbody>
<tr>
<td>L. Latynina</td>
<td>9</td>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>T. Ono</td>
<td>5</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>P. Nurmi</td>
<td>9</td>
<td>3</td>
<td>0</td>
</tr>
<tr>
<td>S. Kato</td>
<td>8</td>
<td>3</td>
<td>1</td>
</tr>
</tbody>
</table>
The Language of Probability

Quick Review

Some events are **impossible**.

Some events are **certain**.

An event that is likely to happen is **probable**.
An event that is unlikely to happen is **improbable**.

You can use a line to show how likely it is an event will happen.

```
  unlikely  likely
impossible     possible     certain
```

The **probability** of an event is a measure of how likely the event is to happen.

Try These

1. Use a word from the box to describe each event.
   a) It will rain meatballs this summer. __________
   b) We will have a fire drill this week. __________
   c) You will walk on the moon. __________

2. Draw counters in the bag so that:
   a) Picking a red counter is likely.
   b) Picking a blue counter is unlikely.
   c) Picking an orange counter is impossible.
Practice

1. Write a sentence using each word.
   a) likely ________________________________
   b) unlikely ______________________________

2. Use the Venn diagram to sort these events.
   A  The sun will set this evening.
   B  A dog will walk down your street today.
   C  Next week will have 7 days.
   D  You will wear a blue shirt tomorrow.
   E  You will see a real pig reading a poem.

3. Suppose you put these cards in a bag and then pull one card out without looking.
   Tell which number:
   a) You are least likely to pick. _______
   b) You are most likely to pick. _______
   c) It is impossible to pick. _______

Stretch Your Thinking

Suppose your brother says, “I’ll roll a number cube. If an odd number comes up, I’ll do the dishes. If an even number comes up, you’ll do the dishes.” Should you take his offer? Explain.

_____________________________________________
_____________________________________________
_____________________________________________
Quick Review

- This spinner has 8 equal sectors. So, there are 8 possible outcomes: landing on 1, 2, 3, 4, 5, 6, 7, 8. Some impossible outcomes are: landing on 9, 10, 11, 12, ...

- This spinner has 2 equal sectors. Landing on 8 is certain.

- This spinner has 8 equal sectors. Landing on 1 and landing on 3 are equally likely. Landing on 4 is less likely than landing on 1 or 2 or 3. Landing on 2 is more likely than landing on 1 or 3 or 4.

Try These

1. a) Which letter is the pointer most likely to land on? __________
   b) On which of 2 letters is the pointer equally likely to land on? __________
   c) Write a statement about the spinner using the words “less likely.” ________________________________
Practice

1. Suppose the pointer on this spinner is spun.
   a) List the possible outcomes.

   ______________________________

   b) Compare the likelihoods of the outcomes.
      Use the words “more likely,” “equally likely,”
      or “less likely.”

   ______________________________

   ______________________________

2. Design a spinner so that:
   ➤ Landing on brown is more likely than landing on blue.
   ➤ Landing on orange and landing on green are
      equally likely.
   ➤ Landing on black is impossible.

3. Yali gets a point if the pointer lands on A, B, or C.
   Patsy gets a point if the pointer lands on D, E, or F.
   The person with more points after 25 turns wins.

   Who is more likely to win? ______________________

   How do you know? ______________________________

   ______________________________

Stretch Your Thinking

Suppose you spin the pointer on this spinner. Compare the
likelihoods of the outcomes.

_______________________________

_______________________________

_______________________________
Conducting Experiments

Quick Review

Spinning a pointer on a spinner is an experiment.

Lester spins the pointer. He records the results of each spin in a tally chart. He conducts the experiment 40 times.

- Number 3 is on the smallest sector. It is less likely that the pointer will land on 3.
- Numbers 1 and 2 are on sectors of the same size. Landing on 1 and landing on 2 are equally likely.
- Number 4 is on the largest sector. It is more likely that the pointer will land on 4.
- All sectors have a number. It is certain that the pointer will land on a number.

<table>
<thead>
<tr>
<th>Number</th>
<th>Tally</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Try These

1. Look at the spinner experiment above.
   a) Which number is more likely to be landed on—1 or 3? _________
      How do you know? ____________________________________________

   b) Which number is less likely to be landed on—2 or 4? _________
      How do you know? ____________________________________________

   c) Which result is more likely—landing on 4 or landing on a number?
      Explain. _____________________________________________________

   d) Which number will never be landed on? _________
      Explain. _____________________________________________________
Practice

1. Work with a partner.
   Place 7 blue and 2 green counters in a bag.
   Take turns to take a counter from the bag and replace it. Record your results in the tally chart.
   Do this 40 times.
   a) Which colour counter is more likely to be taken? _____________________
      Do your results match your answer? Explain.
      ________________________________________________________________
   b) Which colour counter is less likely to be taken? ______________________
      Do your results match your answer? Explain.
      ________________________________________________________________
   c) Which colour counter will never be taken? __________________________
      Do your results match your answer? Explain. ________________________
      ________________________________________________________________

2. Work with a partner.
   Roll a number cube 40 times.
   Record your results in the tally chart.
   Describe the likelihood of each event:
   a) rolling a 4 _______________________
   b) rolling a 10 _____________________
   c) rolling a number less than 5 ________
   d) rolling a number _________________

Stretch Your Thinking

Player A gets a point if the pointer lands on a multiple of 2.
Player B gets a point if the pointer lands on a multiple of 3.
Player C gets a point if the pointer lands on a multiple of 5.
Who is likely to win? Explain.
__________________________________________________
__________________________________________________

<table>
<thead>
<tr>
<th>Number</th>
<th>Tally</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Blue</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Green</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Number</th>
<th>Tally</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Quick Review

Geraldine designed an experiment with a spinner. She designed it so that landing on A was more likely than landing on B.

Sam spun the pointer and recorded the results. He did this 25 times. Here are the results.

The pointer landed on A more often than on B. The experiment turned out the way Geraldine expected.

Try These

1. Colour each spinner so that:

   A landing on red is more likely than landing on yellow.
   B landing on green and landing on purple are equally likely.
   C landing on brown is impossible.
   D landing on orange is less likely than landing on blue.
Practice

1. Design a spinner so that:
   - The pointer landing on black is least likely.
   - The pointer landing on blue is most likely.
   - The pointer landing on yellow and landing on green are equally likely.
   - The pointer landing on red is impossible.

2. You will need 20 blank cards and a paper bag. An experiment is taking a name card from the paper bag without looking. Design an experiment so that taking a girl’s name is more likely than taking a boy’s name. Explain what you did.

3. Conduct the experiment in question 2 to see if it works the way you expect. Record your results in the tally chart. Write about how well the experiment worked.

Stretch Your Thinking

- Colour the spinner using 4 colours. Design an experiment using your spinner. Describe the results you expect.

- Conduct the experiment. Did you get the results you expected? Explain.
A shape is **translated** when it moves along a straight line from one position to another. The movement is a **translation**, or a slide. The shape does not turn. When we draw the shape in its new position, we draw a **translation image** of the shape.

This shape has been translated 2 squares right and 2 squares down. Whenever you describe a translation, say how many squares left or right, and then say how many up or down.

**Translation arrows** join matching points on the shape and its **image**. The shape and its image face the same way.

---

**Try These**

1. Do these pictures show translations? Write **Yes** or **No**.

   a) [Image]

   b) [Image]
Practice

1. Translate each shape. Draw the image and a translation arrow.
   a) 3 squares right and 2 squares up
   b) 4 squares left and 2 squares down

2. Translate the shape three times. Draw the images and the translation arrows.
   Label your translations A, B, and C.

Stretch Your Thinking

How would you describe your translations in question 2?
Quick Review

When a shape is reflected in a mirror, we see a reflection image.

A point and its image are the same distance from the line of reflection.

A shape and its reflection face opposite directions.

A reflection is sometimes called a flip.

Try These

1. Do these pictures show reflections? Write Yes or No.

   a) _______

   b) _______

   c) _______

   d) _______
Practice

1. Draw each reflection image.
   a) 
   b) 

2. Work with a partner.
   Draw a line of reflection in part a.
   Draw a shape on one side of the line of reflection.
   Have your partner draw its reflection image.
   Repeat for part b, but switch roles.

   a) 
   b) 

Stretch Your Thinking

The top shape shown here is a reflection image of the bottom shape.
Draw the line of reflection.
Quick Review

A rotation is a turn about a point of rotation.

When we show the shape in its new position, we draw a rotation image of the shape.

The rotation can be clockwise about a vertex V:

The rotation can be counterclockwise about a vertex V.

This triangle has rotated a \( \frac{1}{4} \) turn clockwise.

This triangle has rotated a \( \frac{1}{4} \) turn counterclockwise.

Translations, reflections, and rotations are all called transformations.

Try These

1. Draw the rotation image of each shape after a \( \frac{1}{4} \) turn, a \( \frac{1}{2} \) turn, and a \( \frac{3}{4} \) turn.
   
   a) \[ \begin{array}{c}
   \text{Shape} \\
   V
   \end{array} \]
   
   b) \[ \begin{array}{c}
   \text{Shape} \\
   V
   \end{array} \]
Practice

1. Draw the rotation image of each shape after each rotation.  
   a) \(\frac{1}{4}\) turn counterclockwise  
   b) \(\frac{1}{2}\) turn clockwise

2. Each picture shows a transformation. Name the transformation.
   a) ______________
   b) ______________

Stretch Your Thinking

Can you tell which transformation has been performed? Explain.
_____________________________________________________________________
_____________________________________________________________________

123
Exploring Different Points of Rotation

Quick Review

A shape can rotate about a point of rotation that is not on the shape.

We can use tracing paper to find the image when we rotate a shape.

- Place the tracing paper so the top right corner is on point P.
- Trace the shape.
- Hold the tracing paper in place with your pencil at point P. Rotate the tracing paper a $\frac{3}{4}$ turn clockwise.
- Note the position of the rotation image.
- Lift the tracing paper and draw the image in place. Label the image.

Try These

1. Use tracing paper.
   Draw each image after a $\frac{1}{4}$ turn clockwise about point P.

   a) 
   b)
### Practice

1. Draw each image after a $\frac{1}{2}$ turn clockwise about point P.
   a) ![Image](image1.png)
   b) ![Image](image2.png)

2. Draw each image after a $\frac{1}{4}$ turn counterclockwise about point P.
   a) ![Image](image3.png)
   b) ![Image](image4.png)

### Stretch Your Thinking

Draw the image of the shape after each rotation about point P:
- $\frac{1}{4}$ turn counterclockwise
- $\frac{1}{2}$ turn clockwise
- $\frac{3}{4}$ turn counterclockwise
Homework doesn't always mean sitting at the table with a paper and pencil. Practise your number sense in the kitchen while supper is cooking, or while driving in the car or at the store with a number sense anywhere at all! Riddle Me

Numbers in columns, numbers in rows;
Start with a few and watch them grow. Some say they're tough, but I can't be fooled. ’Cause I hunt for patterns... that's my secret tool.

I'm thinking of a number...

It has 350 tens and 5 ones.

Can you guess what it is?

Put these together and you'll never be stumped when you add the digits in each answer.

But wait... there's more! What do you notice when you add the digits in each answer?

Tens place in the answer?

Catch the pattern! What do you notice about the tens place in the answer?

What do you notice about the tens place in the answer?

Nifty Nines

I ask myself good questions on my noble pattern quest.

Self, I say, look carefully... What's the difference?

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Self, I say, look carefully... What's the difference?

No, wait, it shrinks by 5. Eureka! This is it!

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What do you notice about the tens place in the answer?
Would You Rather?
Imagine that you just got a new job for 1 month. Your employer gave you a choice of how you would be paid.

1. $5000 for the month
2. 1¢ the first day, then your pay would double each day until the month was up.

You gave it a quick think and, of course, jumped at the first choice... $5000 for just one month is a lot of money!

Did you make a good choice? Check it out!

On the Road Again!
You are heading out on another trip!

Is there a pattern to where distance signs are placed along the highway?

Find out by calculating the difference in distance between one sign and the next.

If there is a pattern, it should show up in the next few signs. Does the location make a difference?

Pick Up the Pattern
Here is a pattern of attached triangles made with toothpicks.

➤ Use toothpicks to copy and extend the pattern.
➤ Copy and complete the table.

<table>
<thead>
<tr>
<th>Figure Number</th>
<th>1</th>
<th>2</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of Toothpicks</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

➤ Write an expression to represent the pattern in the number of toothpicks.
➤ Find how many toothpicks would be needed to make the 28th figure.

Who invented fractions?
Henry the English

Who helped him?
Louis the Sixteenth

What do you call people in favour of tractors?
Pro-tractors

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Odd One Out
Once you figure out the strategy to guarantee a win, you'll be able to stump just about anyone!

Find a partner, then set out 13 counters (buttons, coins, etc.) in a line. 12 of them must be the same and 1 different. In turn, starting with the first counter, you may take 1 or 2 counters (the choice is yours). If you take 2 counters, the remaining counters must be the same. Example: In the first turn, you take 2 counters. On the second turn, you may take 1 counter.

Hint: Work backwards. Think about what you want for a number. Are you forced to take the different colored counter? If yes, you lose. The idea is to not get into a position where you must take a counter you don’t want. Which color (white or red) do you want to be? If you are using a red counter, you may take 2 counters. Be careful! You may lose if you make a mistake.

Use what you already know!

➤ Any multiple of 3 (12, 24, 36, etc.) is a multiple of 6.
➤ Any number x 1 is the same number.
➤ Any number x 5 is the same number.
➤ Any number x 10 is the same number.

Once you figure out the strategy to guarantee a win, you'll be able to stump just about anyone.

A Speeding Pencil
Faster than a Speeding Pencil!
Would you believe that you can multiply all of the numbers on your phone pad together in your head faster than I can do it on a calculator? It’s true! But how can that be?

Use what you already know!

➤ Any number x 0 is 0.
➤ Any number x 1 is the same number.
➤ Any number x 9 is the same number.

How Many Are There Really?

Use what you already know!

Do you really need to memorize...

➤ Any number x 30? Probably not… cross them off.
➤ Any number x 31? Probably not… cross them off.
➤ Any number x 32? That’s just like adding doubles.
➤ Any “turn around” fact (3 x 4 is the “turn around” of 4 x 3)? That gets rid of about half right there.

How many now? Are you surprised?

<table>
<thead>
<tr>
<th>90</th>
<th>80</th>
<th>70</th>
<th>60</th>
<th>50</th>
<th>40</th>
<th>30</th>
<th>20</th>
<th>10</th>
<th>0</th>
</tr>
</thead>
<tbody>
<tr>
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</tr>
</tbody>
</table>

Challenge someone to a duel and try it out!
In the Bag

You’ll need:
➤ a 100-chart (page 5)
➤ 12 small paper squares numbered 1 to 12
➤ 20 buttons (10 of one colour and 10 of another)
➤ a paper bag

The object of this game is to get rid of your buttons first!

➤ Place all number squares in the paper bag.
➤ In turn, take three squares from the bag…
   No peeking!
➤ Multiply any two or three of the numbers together.

\[
\begin{array}{ccc}
2 & 8 & 5 \\
2 \times 5 & \text{or} & 2 \times 8 & \text{or} & 5 \times 2 \times 8
\end{array}
\]

➤ With one of your buttons, cover the number on the 100-chart that represents the product you made.
➤ Now it’s the next player’s turn.

No two buttons can share the same square.
If you can’t play, you’ll have to wait for your next turn.

Clean up all of your buttons first and you are the champ!

Longing to Belong

Find 3 more numbers that belong in this group.
How do you know they belong?

\[
\begin{array}{cccccccccc}
176 & 297 & 363 & 583 & 451 & 396 & 275
\end{array}
\]
Check It Out!

Find some bottles, jars, jugs, or cans whose capacities are given in millilitres or litres. Make a chart that shows the contents and capacities of each container. Then answer these questions.

1. How many of these containers of cross will you use in a year?
2. How many of these bottles have a capacity of 4.5 L?
3. How many of these jugs have a capacity of 1.9 L?
4. How many of these cans have a capacity of 3.75 L?

Floss Those Pearly Whites!

Suppose you use 30 cm of dental floss each day. How many of these containers of floss will you use in a year?

Smart Alec

Alec only had a 3-L pitcher and a 5-L pitcher. He managed to measure out exactly 1 L of cider. How did that smart Alec do it?

Rules! Rules! Rules!

Sometimes I feel befuddled.

Rules. Which one is right for the job at hand? Which one was it that I'm not supposed to mention? Which one am I sure and then I'm not sure whether I should I want? Rules, rules, rules! How do I keep all of them straight?

Kids Rule!

I'm sure and then I'm not sure. My own rules are appearing through my new math lens. How do I know? How many places? Where do I start? Which comes next? Is this right? Where do I put it?
Mathematics Acrobatics

Try this number trick out on a friend!

Ask her to…
➤ choose a number
➤ add 3
➤ multiply by 2
➤ add 4
➤ divide by 2
➤ subtract the original number

Now tell your friend that her answer is 5!

Aren’t you amazing! Does it work with any number? What about decimal numbers?

You can make up your own number tricks if you understand how they work... “Mind pictures” can help!

✓ 25
✓ + 3
✓ × 2
✓ + 4
✓ ÷ 2
✓ subtract the original number

Now make up some of your own!

Fraction Action

You’ll need:
➤ 24 counters for each player
➤ paper clip to use as a pointer

The object of the game is to have the most counters after 10 turns.

➤ In turn, spin the pointer on the spinner. Name the fraction.
➤ If you can take exactly that fraction of your opponent’s counters, take them and add them to your pile.
➤ If you can’t take the exact fraction, don’t take any counters.
➤ Play for 10 rounds.
Think about it!

To each digit, the first player to get to 1000 wins.

How many different fractions less than 1 can you make with these numbers?

9 7 5 1 3

What can you say about the volume as the shape changes?

Bring It to Zero!

You’ll need:

➤ 2 or more players
➤ You’ll need:

How can you tell without unrolling it?

around your room more than once?

Is there enough in a small container to go all the way?

Fractured Fractions

The object of this game is to bring each of the digits to 0. Each turn, you choose a different digit or work on the same digit. Whatever number you choose, subtract it from your current total. The next player must choose a different digit or work on the same digit. Once you have subtracted the chosen digit, the next player must choose another digit or work on the same digit. Continue until each digit is brought to 0.

Try this experiment!

The next time you have an empty paper towel tube:

Varying Volumes

The next time you have an empty paper towel tube:

➤ Cover one end of the tube with tape.
➤ Fill the tube with rice or beans.
➤ Using a measuring cup, pour the contents of the tube into your new container. Can you pour all of the contents into your new container?

Now try it the other way:

one. The player to get the least 0 wins that round.

Enter a 6-digit number below 500 and take turns adding.

Once you have entered your turn is done and the next player may choose a different digit or work on the same digit. The next player may choose a different digit or work on the same digit. Continue until each digit is brought to 0.

To top and tape it up.

Now fill it back up from bottom.

Mark the top and bottom edges. It should look like a rectangle.

Fill the tube with rice or beans.

Cover one end of the tube with tape.

Cut the tube along its length and lay it flat.


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G5_MAH2 SE.qxd 6/27/08 9:45 AM Page 3

G5_MAH2 SE.qxd 6/27/08 9:45 AM Page 6
Roll to a Whole!

You'll need:
➤ 2 number cubes
➤ 2 copies of the grid on page 5
➤ crayons or markers

The goal is to be the first to colour one whole grid.

On your turn:
➤ Roll one number cube. This will tell you how many tenths you may colour on your grid.
➤ Roll the second number cube. This will tell you how many hundredths you may colour on your grid.
➤ Colour them and say how much of your whole grid is coloured.
➤ Colour them and say how much of your whole grid is coloured. Record that decimal number on a piece of paper and... that's the end of your turn!

Does it sound too easy?
Here are a couple rules you must obey:
1. If you forget to say your decimal number aloud, your partner gets an extra turn.
2. If you roll doubles, you must colour that amount on the other player's grid.

Bonus!
If you can also say how much of your grid is left to colour, give yourself a bonus of 5 more hundredths.

Colour your grid first to be the decimal champ!
Super Squares

Draw a nice neat square and mark 3 midpoints.

Connect the points as shown and cut along those lines.

You'll be left with a pentagon and 2 triangles.

How many different shapes can you make with these 3 pieces? Can you make one that looks like an animal?

More circles?

6 circles?

4 circles?

2 circles?

Mirror, Mirror...

Where could you place a straight-sided mirror so that you could see:

My closet is a virtual kingdom in 3-D.

My hamper is rectangular.

In that little orange paper box I see a prism in a tissue box and not see three-dimensional shapes no more. I can look around there's nowhere I can look around.

A hat from Lee's party. I think my sock is a cylinder.

My closet is a virtual kingdom in 3-D.

In that little orange paper box I see a prism in a tissue box.

My hamper is rectangular. No accident. I see a pyramid in the hamper.

I see a prism in a tissue box and not see three-dimensional shapes no more. I can look around there's nowhere I can look around.

Distractions in 3-D:

I can't escape this madness. Of the hexagonal family. My bedposts are all perpendicular to each other.

I think my sock is a cylinder.

A hat from Lee's party. I think my sock is a cylinder.

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Bag It!

You’ll need:
➤ a paper bag
➤ coloured counters or buttons

Suppose you take one counter from the bag without looking, then replace it.

Design an experiment so that:
• You are more likely to take a green counter than a blue counter.
• Taking white is impossible.
• Taking a green counter and taking a red counter are equally likely.

How many counters of each colour would you put in the bag?

Conduct your experiment. Record your results.

As the Shape Turns

Work with a partner.

Take turns:
➤ Draw a shape on the grid.
Choose a point outside the shape.
Rotate the shape about the point.
Draw its rotation image.
➤ Have your partner identify the rotation, including:
  – the point of the rotation
  – the fraction of the turn
  – the direction of the turn.
Who Knows?

Semaphore is an alphabet signalling system based on holding flags, with the arms at different angles, to represent letters or numbers.

Semaphore

First to clean up wins!

1. If you roll a 6, miss your turn.
2. If you roll a 3, give the other player 3 rhombuses to add to his or her collection.
3. Roll the number cube to add to his or her collection.

On your turn:

Roll the number cube:

1. If you roll a 6, miss your turn.
2. If you roll a 3, give the other player 3 rhombuses to add to his or her collection.
3. Roll the number cube to add to his or her collection.

Take 2 rhombuses from the other player.

Special Rules

Draw 2 polygons on light cardboard.

To begin, each player joins 2 rhombuses to make 5 hexagons.

Trace and cut your polygons.

Create a design by flipping, sliding and turning the rhombus.

Tell how much is left.

You must say it 2 ways.

Draw a polygon on light cardboard.

This will tell you how many rhombuses you may discard.

Colour your design.

Make it as attractive as you can.

The images should touch but not overlap.

Mix Them Up!

You’ll need:

➤ copies of the rhombus shown below
➤ a number cube

The object of this game is to be the first to clear away all of your pieces.

With only acute angles?

What words can you make?

Look up the code on the web.

To represent letters or numbers.

with the same different angles.

Semaphore is an alphabet signalling system.

Design It!

Draw a polygon on light cardboard.

Create a design by flipping, sliding and turning the rhombus.

Tell how much is left.

You must say it 2 ways.

I have 1/3

3

more!
I Wonder…
Do people with the biggest hands also have the biggest feet?
Conduct your own survey to find out!

➤ Make some copies of the 1-cm grid on page 5 (or use graph paper).
➤ Find some willing participants.
➤ Trace each person's hand and foot on the grid (you may have to join sheets together).

What is the area of each hand and each foot?
How will you count the part-squares?
Displaying your information in a double bar graph will give you an instant picture of the answer!

Show your graph to someone and tell them what you've found out!